

# Learning-Driven Linguistic Evolution

Lisa Pearl

Cognitive Sciences, UC Irvine

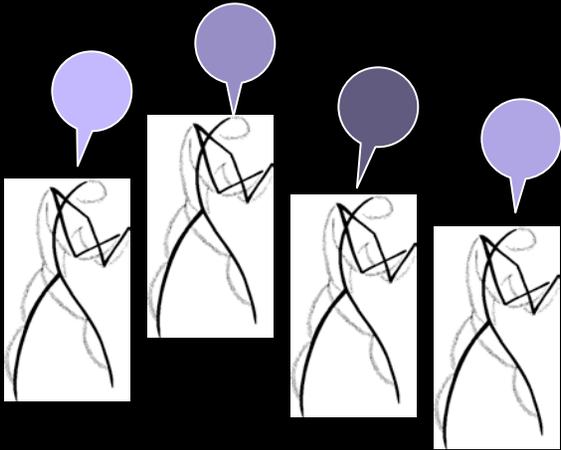
March 16, 2008

Evolution of Psychological Categories Workshop

Institute for Mathematical Behavioral Sciences

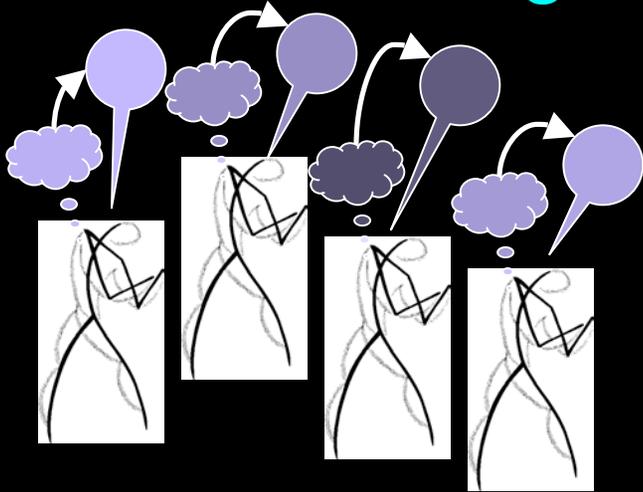
UC Irvine

# Linguistic Evolution, In Brief



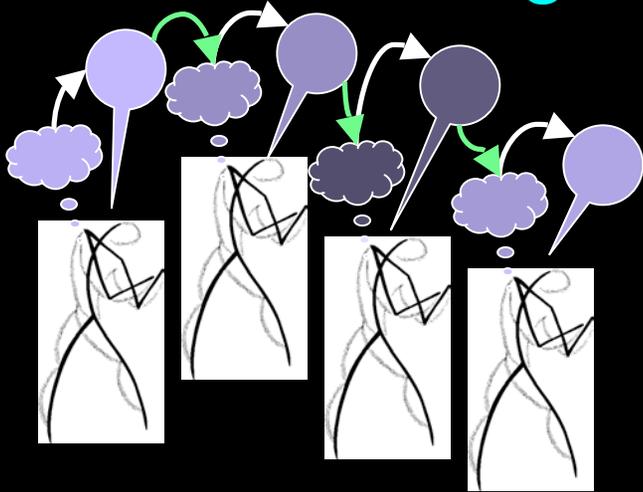
Linguistic knowledge is transmitted in a population via interaction with other speakers in the population.

# Linguistic Evolution, In Brief



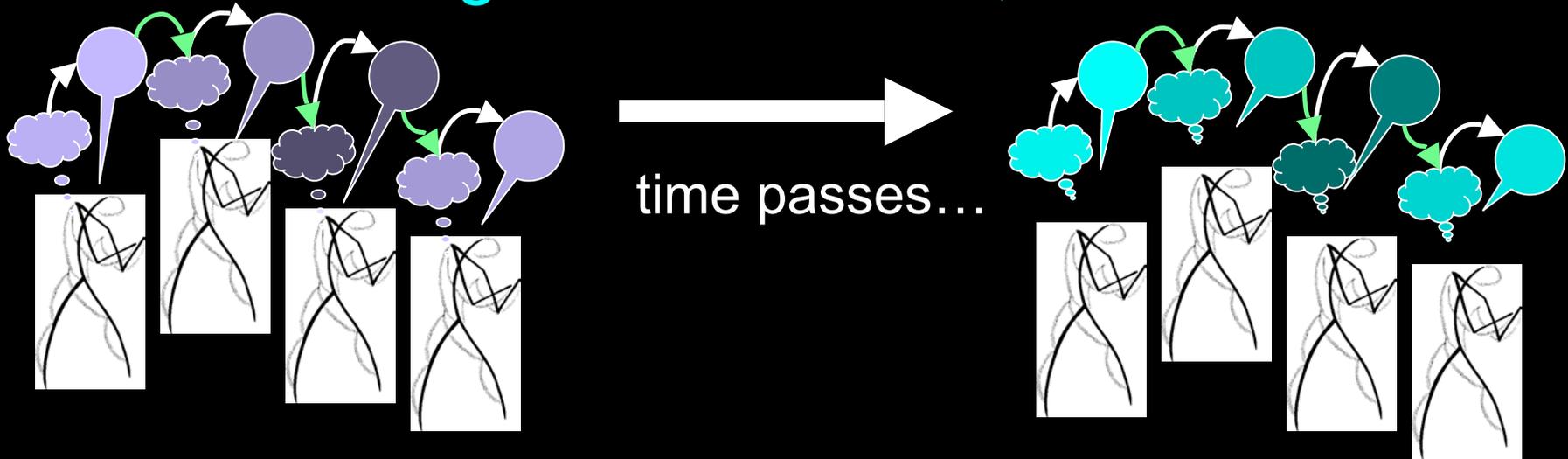
The information speakers transmit (observable data) is based on their own linguistic knowledge.

# Linguistic Evolution, In Brief



Speakers **adjust their linguistic knowledge** based on the observable (and encountered) data from other population members.

# Linguistic Evolution, In Brief



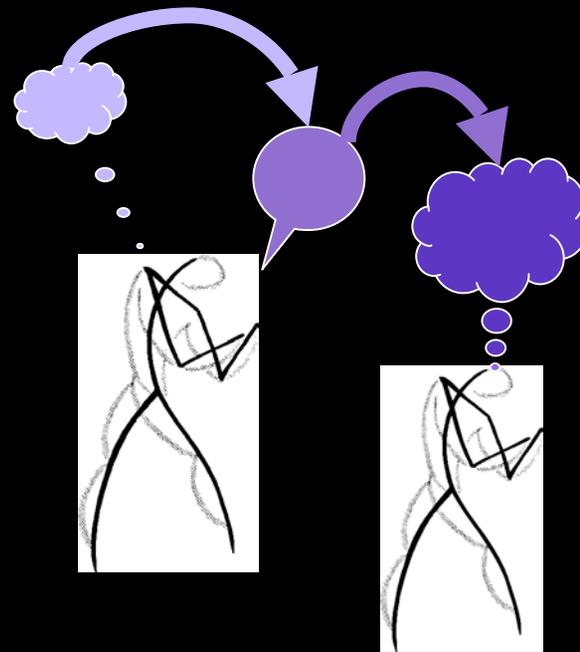
Population-level changes over time depend on what information speakers pass to subsequent generations and how that information is integrated into an individual's linguistic knowledge.

# Integrating Linguistic Information

Not all linguistic knowledge is created equal

Some knowledge can be altered throughout an individual's life

(example: vocabulary)

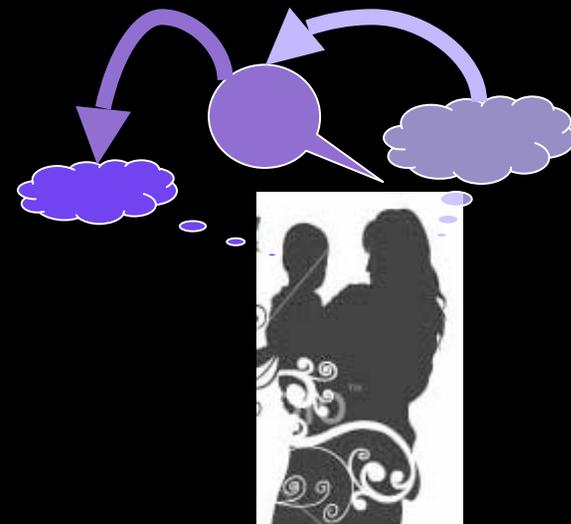


# Integrating Linguistic Information

Not all linguistic knowledge is created equal

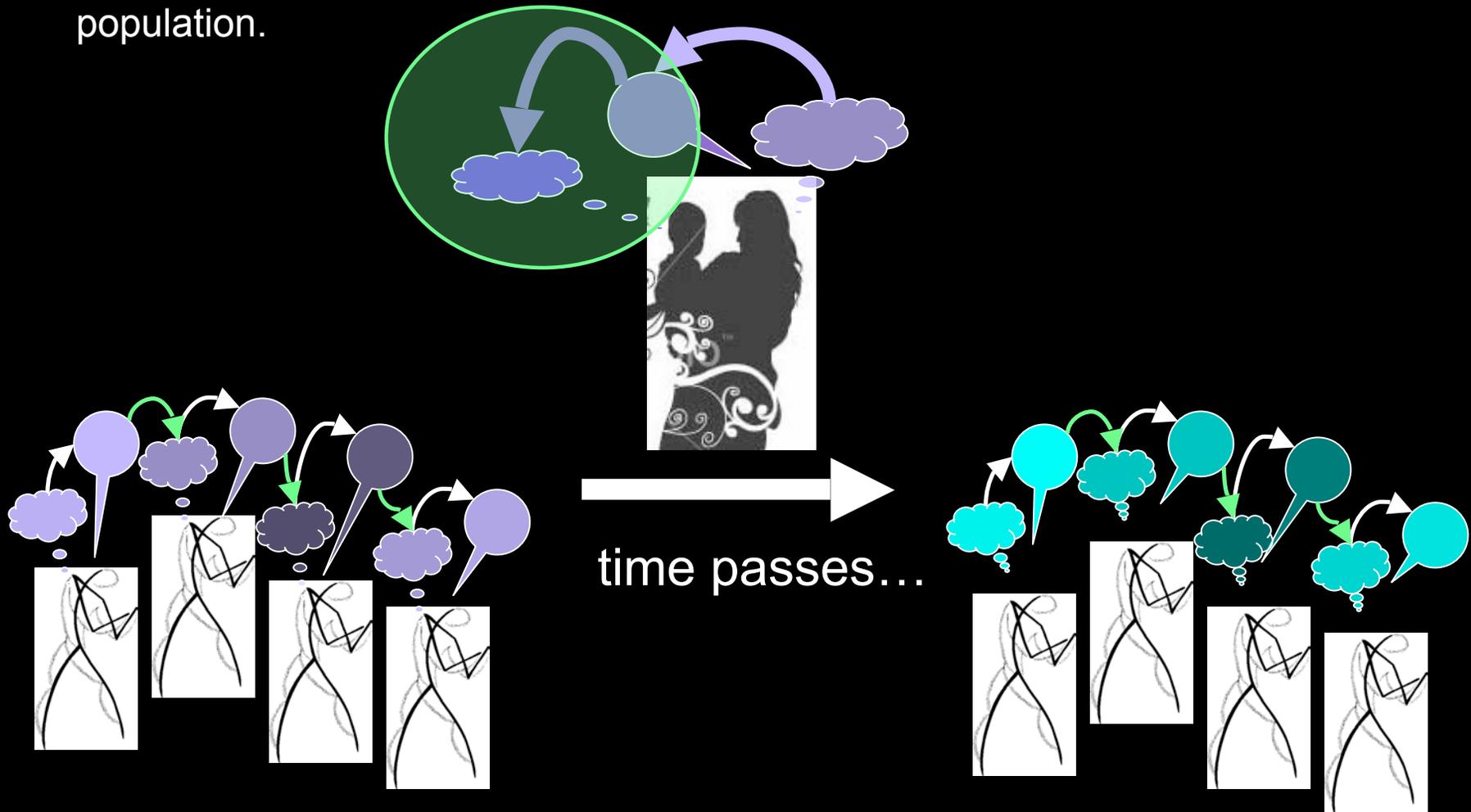
Some knowledge can be altered only during the early stages of an individual's life

(example: word order rules)



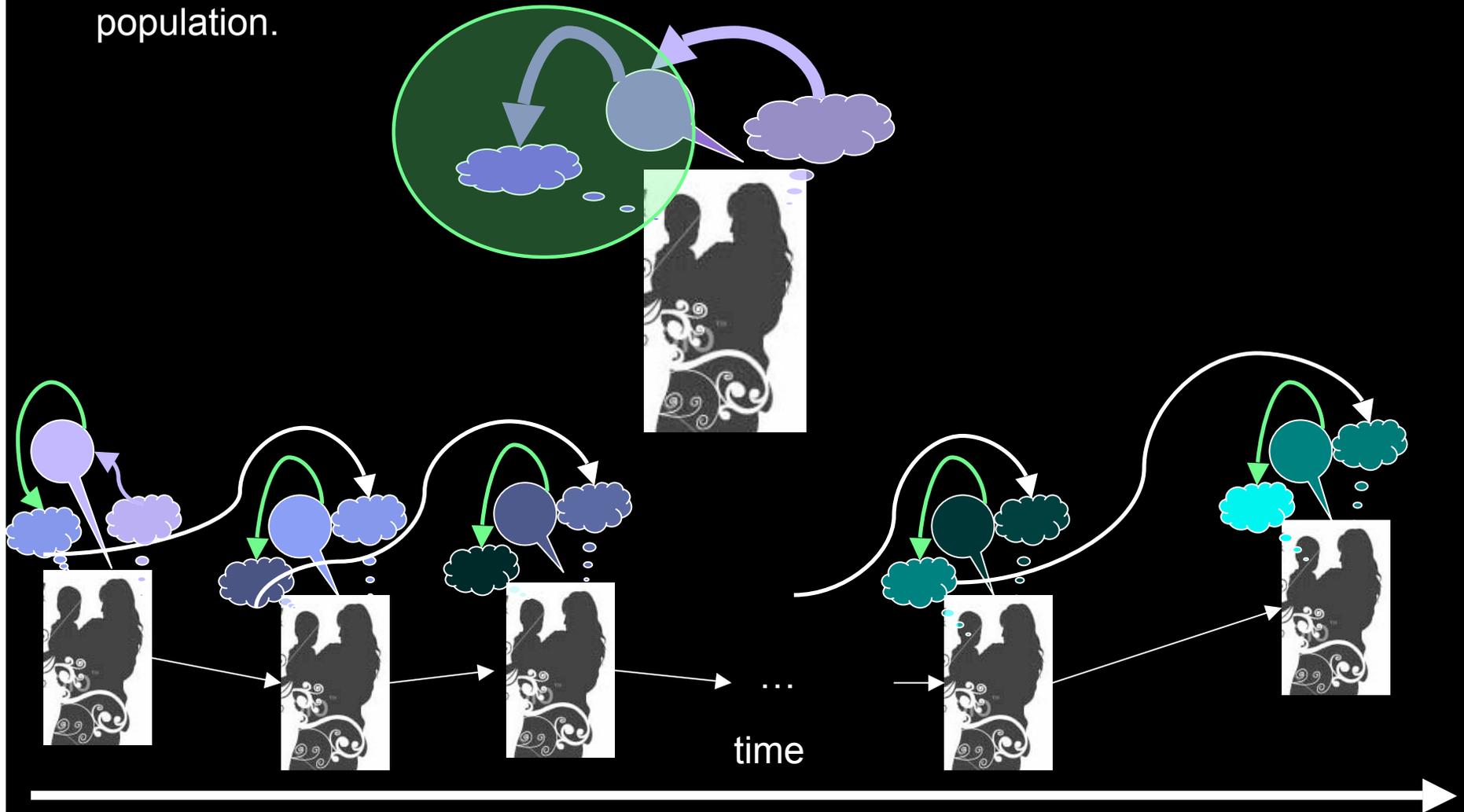
# Change to knowledge that is alterable early

Implication: The way in which young learners integrate linguistic information (along with the data available) determines the linguistic composition of the population and the speed at which the linguistic knowledge evolves within the population.



# Change to knowledge that is alterable early

Implication: The way in which young learners integrate linguistic information (along with the data available) determines the linguistic composition of the population and the speed at which the linguistic knowledge evolves within the population.



# Road Map

## I. Individual Language Learning

The Nature of Linguistic Knowledge  
Individual Learning Framework

## II. Linguistic Evolution: Case Study

Old English Word Order

Modeling Individuals (Pearl & Weinberg 2007)

Modeling Populations

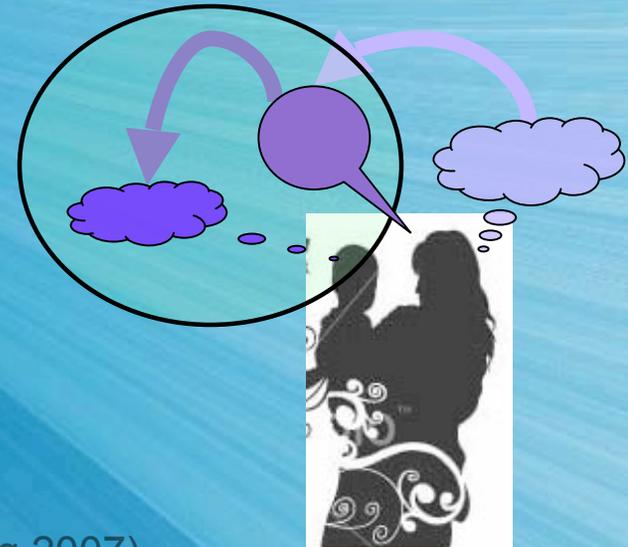
Issues in Empirical Grounding

Selective Learning Biases

# Road Map

- I. Individual Language Learning  
The Nature of Linguistic Knowledge  
Individual Learning Framework

- II. Linguistic Evolution: Case Study  
Old English Word Order  
Modeling Individuals (Pearl & Weinberg 2007)  
Modeling Populations  
Issues in Empirical Grounding  
Selective Learning Biases

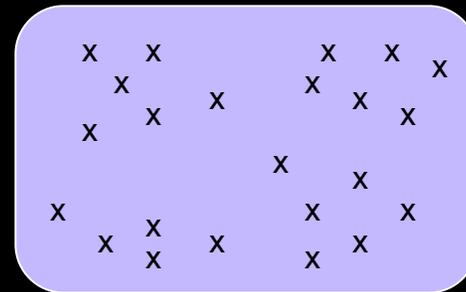


# The Nature of Linguistic Knowledge

Different aspects: **more** and **less** transparent from data

## Categorization/Clustering

Ex: What are the contrastive sounds of a language?

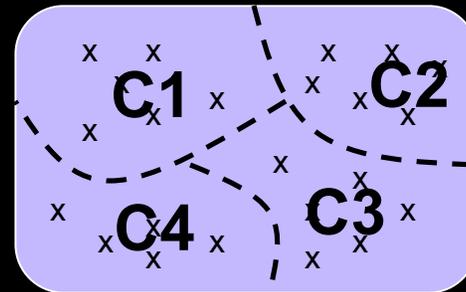


# The Nature of Linguistic Knowledge

Different aspects: **more** and **less** transparent from data

## Categorization/Clustering

Ex: What are the contrastive sounds of a language?

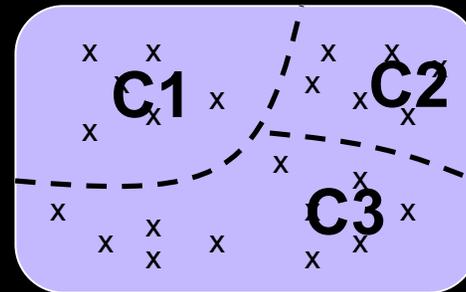


# The Nature of Linguistic Knowledge

Different aspects: **more** and **less** transparent from data

## Categorization/Clustering

Ex: What are the contrastive sounds of a language?

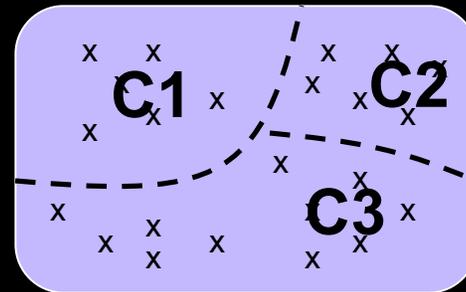


# The Nature of Linguistic Knowledge

Different aspects: **more** and **less** transparent from data

## Categorization/Clustering

Ex: What are the contrastive sounds of a language?



## Extraction

Ex: Where are words in fluent speech?

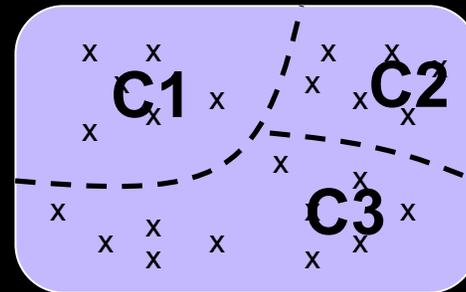
húwzəfréjðəvðəbɪgbæ'dwə'lf

# The Nature of Linguistic Knowledge

Different aspects: **more** and **less** transparent from data

## Categorization/Clustering

Ex: What are the contrastive sounds of a language?



## Extraction

Ex: Where are words in fluent speech?

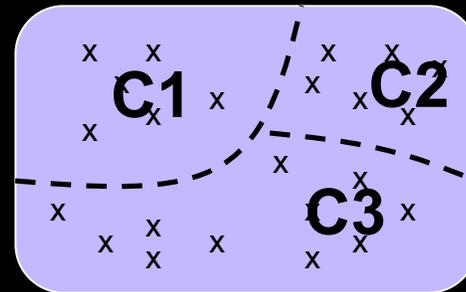
**húwz əfréjd əv ðə bíg bæ'd wə'lf**  
who's afraid of the big bad wolf

# The Nature of Linguistic Knowledge

Different aspects: **more** and **less** transparent from data

## Categorization/Clustering

Ex: What are the contrastive sounds of a language?



## Extraction

Ex: Where are words in fluent speech?

*húwz əfréjd əv ðə blg bæ'd wə'lf*  
who's afraid of the big bad wolf

## Mapping

What are the word affixes that signal meaning (e.g. past tense in English)?

blink~blinked    confide~confided

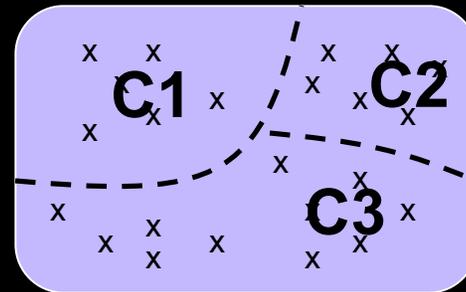
drink~drank

# The Nature of Linguistic Knowledge

Different aspects: **more** and **less** transparent from data

## Categorization/Clustering

Ex: What are the contrastive sounds of a language?



## Extraction

Ex: Where are words in fluent speech?

húwz əfréjd əv ðə blg bæ'd wə'lf  
who's afraid of the big bad wolf

## Mapping

What are the word affixes that signal meaning (e.g. past tense in English)?

blink~blinked      confide~confided  
blɪŋk blɪŋkt      kənfaɪd kənfaɪdəd

drink~drank  
drɪŋk dreɪŋk

# The Nature of Linguistic Knowledge

Different aspects: **more** and **less** transparent from data

**Complex systems:** What is the generative system that creates the observed (structured) data of language (ex: syntax)?

**syntax = word order rules**

**Learning problem: many ways to generate observable data**

# The Nature of Linguistic Knowledge

Different aspects: **more** and **less** transparent from data

**Complex systems:** What is the generative system that creates the observed (structured) data of language (ex: syntax)?

**syntax = word order rules**

**Learning problem: many ways to generate observable data**

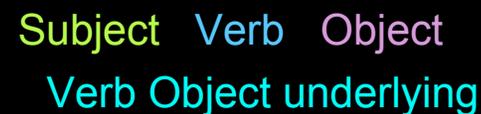
Observable data: word order    **Subject**   Verb   **Object**

Generative system: syntax

Kannada



English



German

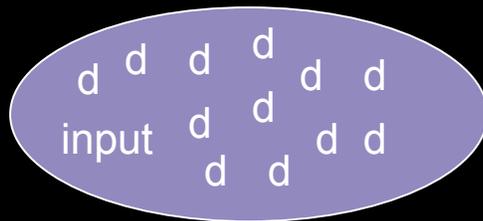


# The individual learning framework: 3 components

(1) Hypothesis space



(2) Data



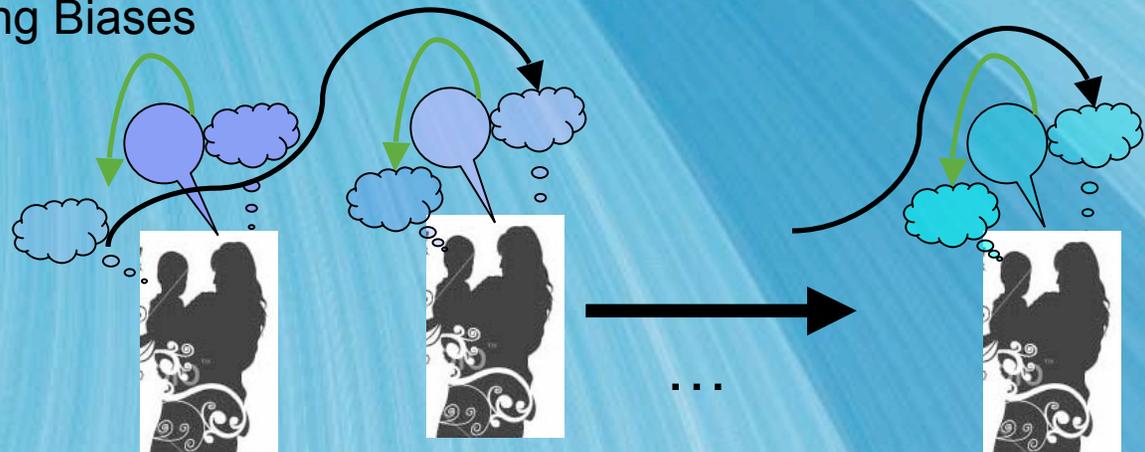
(3) Update procedure



# Road Map

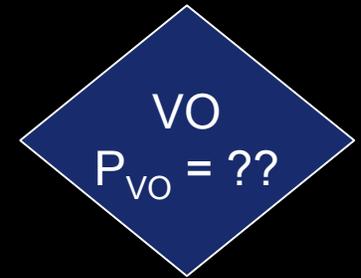
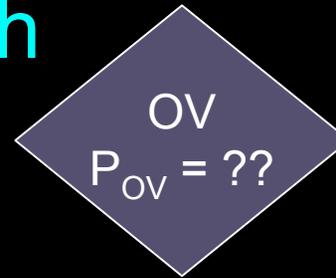
I. Individual Language Learning  
The Nature of Linguistic Knowledge  
Individual Learning Framework

II. Linguistic Evolution: Case Study  
Old English Word Order  
Modeling Individuals (Pearl & Weinberg 2007)  
Modeling Populations  
Issues in Empirical Grounding  
Selective Learning Biases

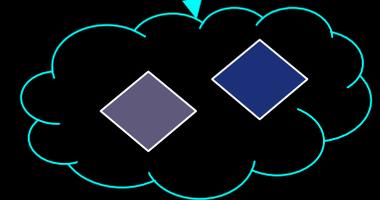


# Old English

Changing Basic Word Order Rule in Old English:  
Object-Verb (OV) vs. Verb-Object (VO) order

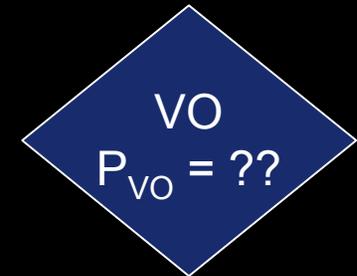
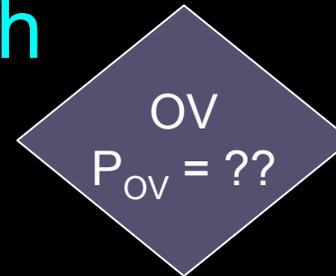


**Individual Knowledge** (underlying probability in speaker's mind):  
probability distribution between OV and VO orders



# Old English

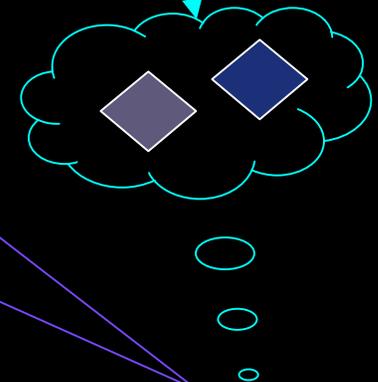
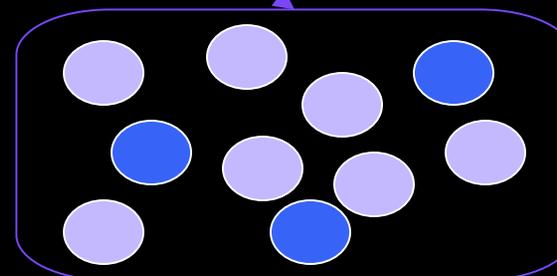
Changing Basic Word Order Rule in Old English:  
Object-Verb (OV) vs. Verb-Object (VO) order



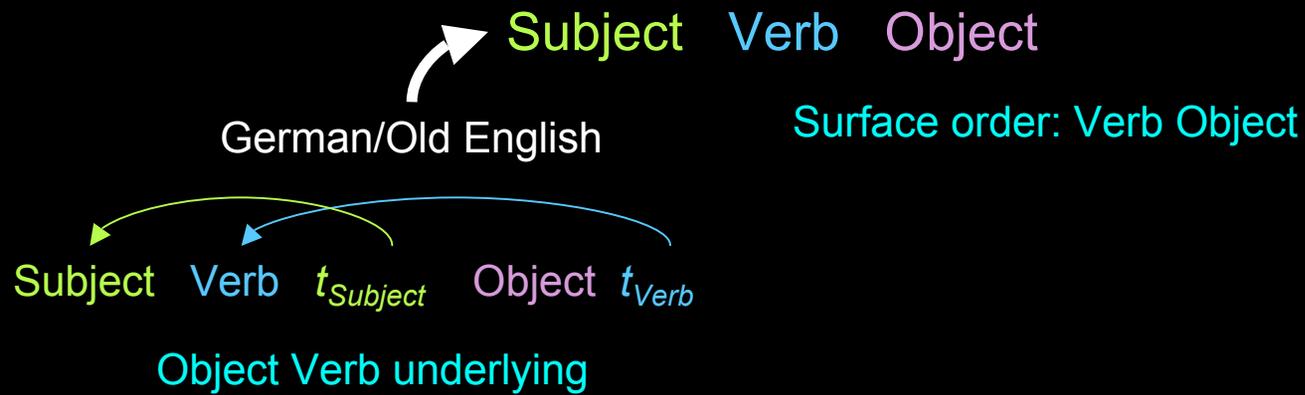
**Individual Knowledge** (underlying probability in speaker's mind): probability distribution between OV and VO orders

**Individual Usage** (observable data for learner): probability distribution between OV and VO orders (not necessarily same one as individual knowledge distribution, from learner's perspective)

Why not?



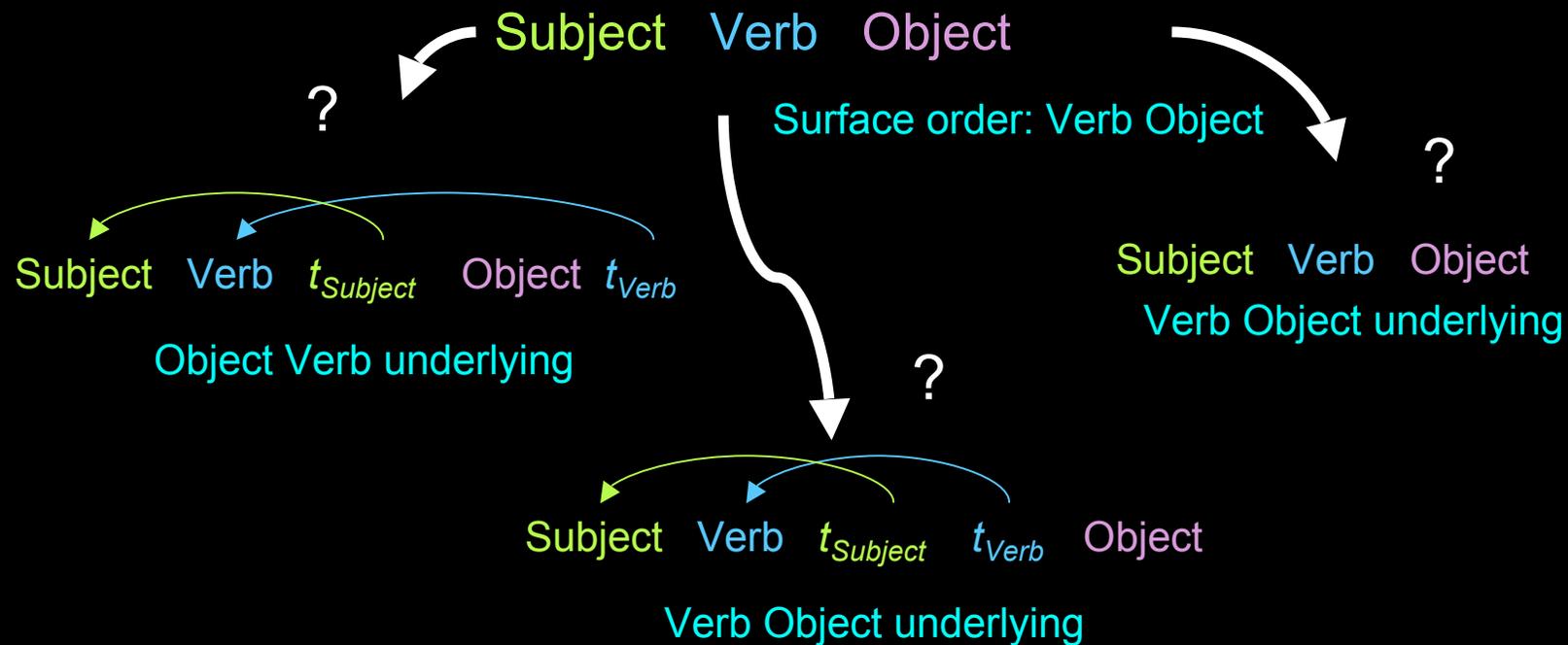
# Underlying Distribution vs. Observable Distribution



Speaker generates utterance



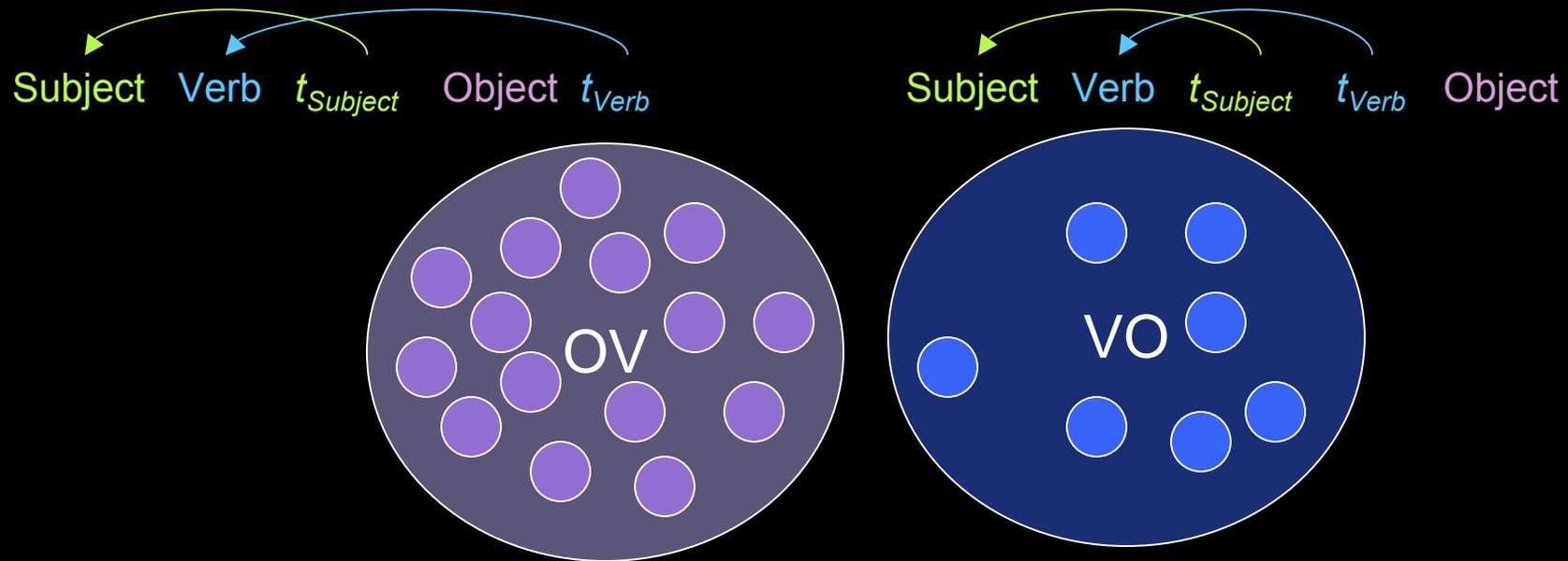
# Underlying Distribution vs. Observable Distribution



Learner interprets utterance



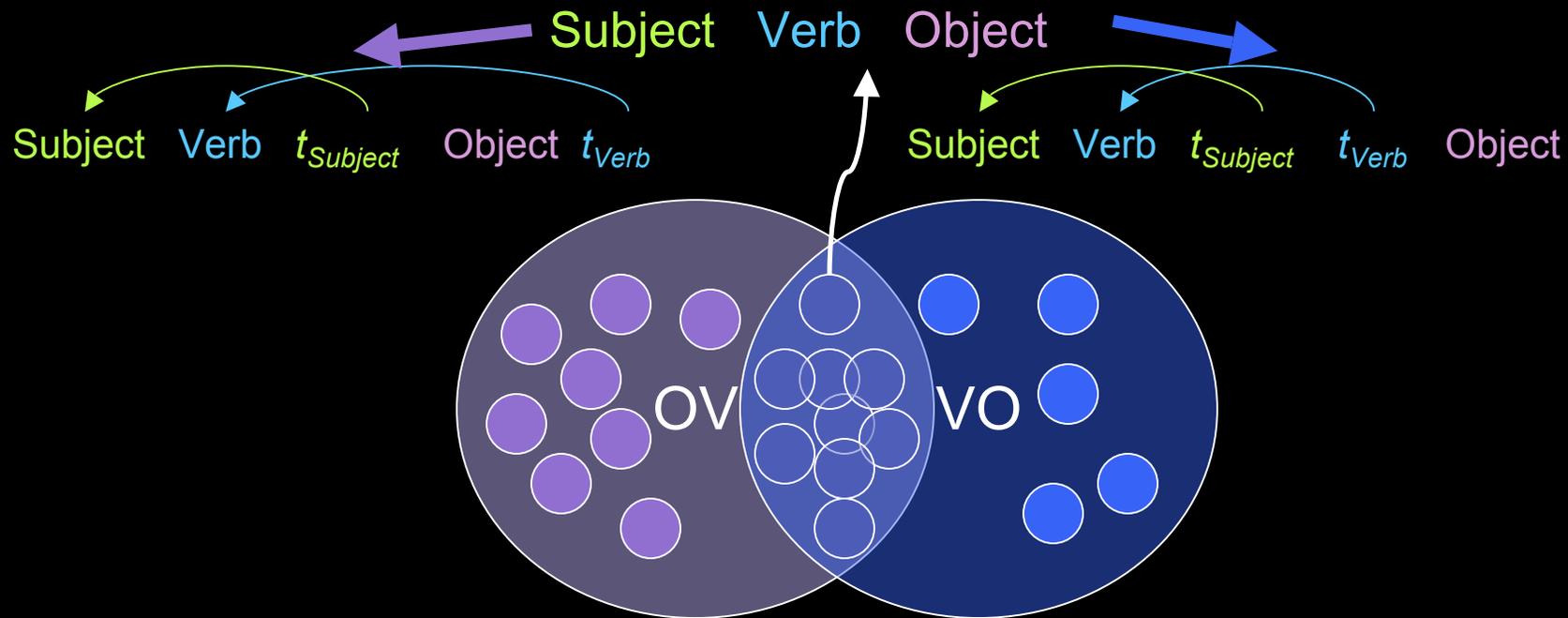
# Underlying Distribution vs. Observable Distribution



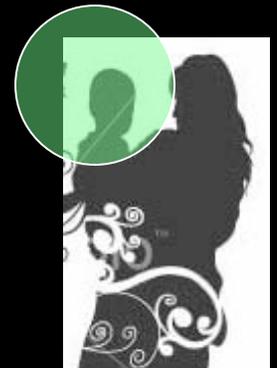
Every utterance generated by speaker is either OV or VO order in the underlying distribution



# Underlying Distribution vs. Observable Distribution

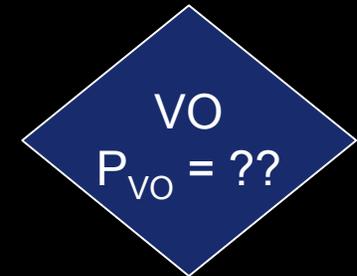
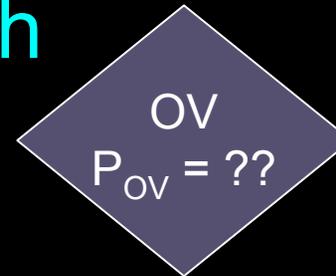


The learner encounters data that is ambiguous between the two options. Distribution depends on learner's interpretation of ambiguous data



# Old English

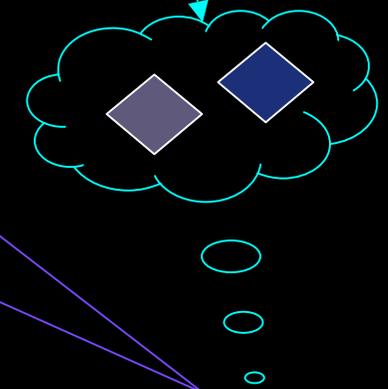
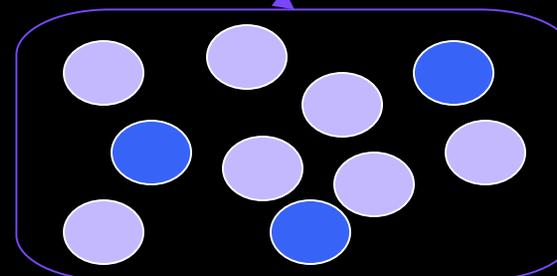
Changing Basic Word Order Rule in Old English:  
Object-Verb (OV) vs. Verb-Object (VO) order



**Individual Knowledge** (underlying probability in speaker's mind): probability distribution between OV and VO orders

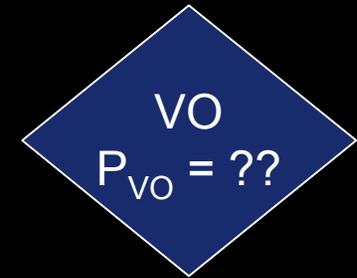
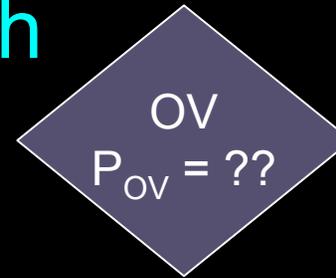
**Individual Usage** (observable data for learner): probability distribution between OV and VO orders (not necessarily same one as individual knowledge distribution, from learner's perspective)

Why not?



# Old English

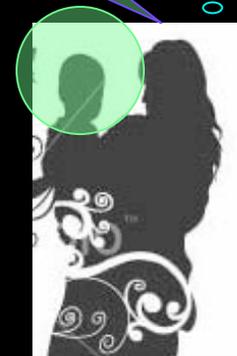
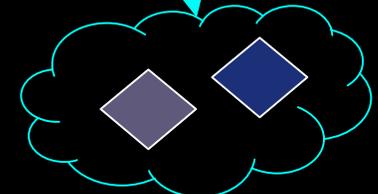
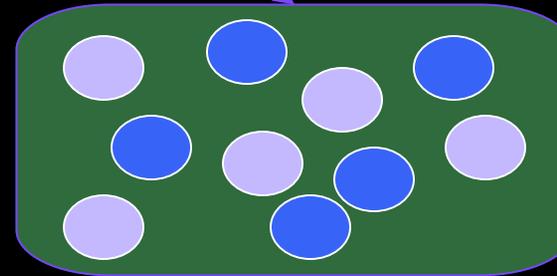
Changing Basic Word Order Rule in Old English:  
Object-Verb (OV) vs. Verb-Object (VO) order



**Individual Knowledge** (underlying probability in speaker's mind): probability distribution between OV and VO orders

**Individual Usage** (observable data for learner): probability distribution between OV and VO orders (not necessarily same one as individual knowledge distribution, from learner's perspective)

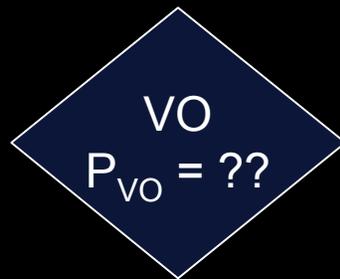
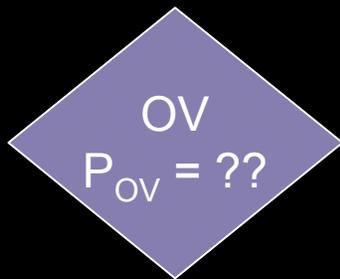
Due to learner interpretation bias



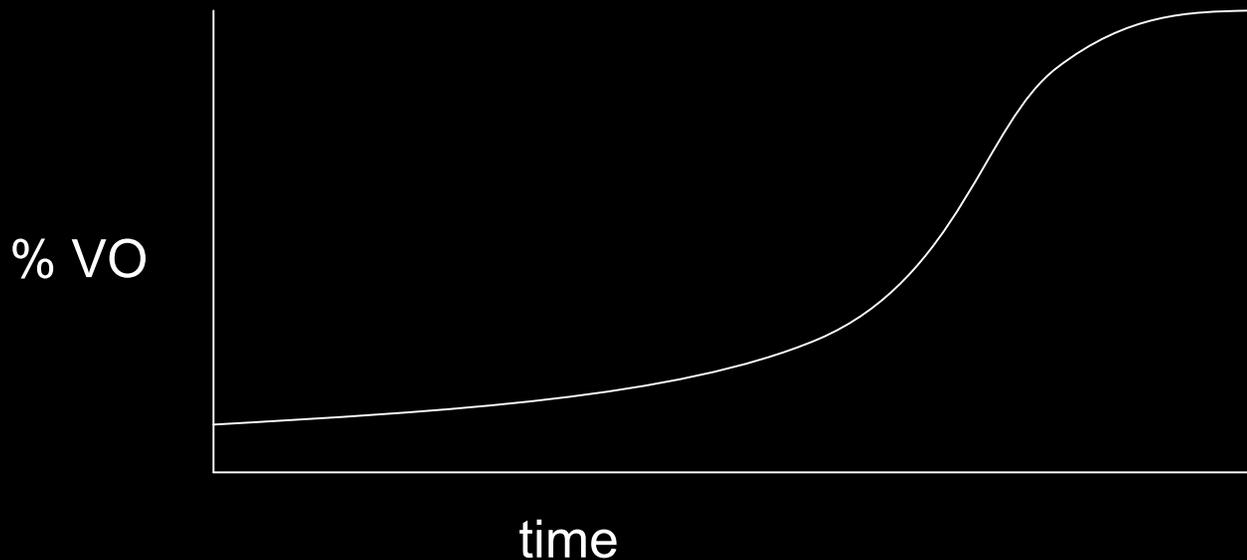
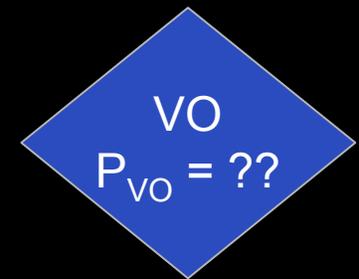
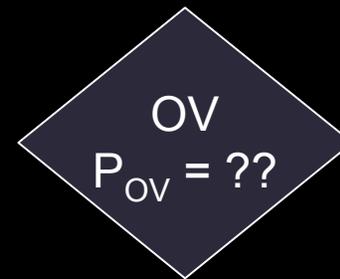
# Old English

Estimates of average individual usage from historical corpora:  
YCOE Corpus 2003; PPCME2 Corpus 2000

~1000 A.D.-1150 A.D.: OV-biased

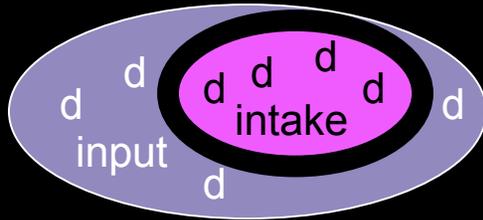


~1200 A.D.: VO-biased



To get this rate of change, young individual learners at each time step must change their probability distribution the exact right amount from the previous population members' distribution

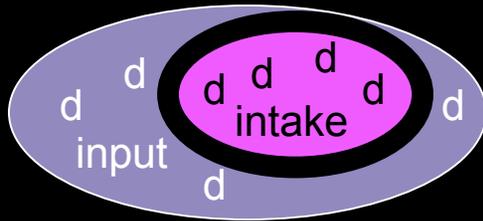
# Modeling Individuals: Learning Biases



**Interpretation Bias:** Use only data perceived as most informative (Fodor 1998, Lightfoot 1999, Dresher 1999).

**Interpretation Bias:** Use only data that is more accessible (perhaps for language processing reasons) (Lightfoot 1991).

# Modeling Individuals: Learning Biases



**Interpretation Bias** : Use only data perceived as most informative: **unambiguous data** (Fodor 1998, Lightfoot 1999, Dresher 1999).

**Interpretation Bias**: Use only data that is more accessible (perhaps for language processing reasons) (Lightfoot 1991).

Learner has heuristics for identifying unambiguous **OV/VO** data, based on partial knowledge of possible adult system rules (Fodor 1998, Lightfoot 1999, Dresher 1999)

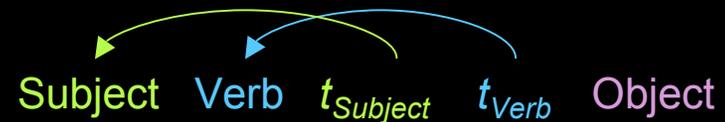
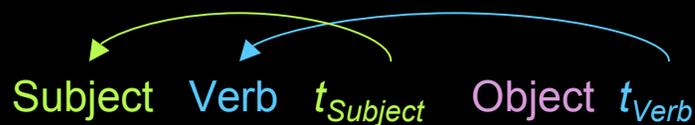
Knowledge of tensed verb movement to 2nd phrasal position of sentence

OV unambiguous data:

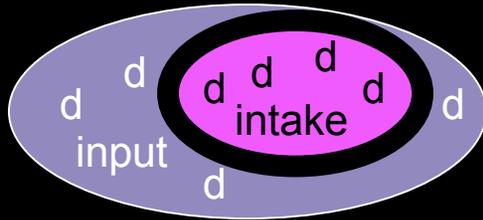
[...]XP ... Object TensedVerb ...  
 ...TensedVerb ... Object Verb-Marker ...

VO unambiguous data:

[...]XP [...]XP ... TensedVerb Object ...  
 ...TensedVerb ... Verb-Marker Object ...



# Modeling Individuals: Learning Biases



**Interpretation Bias:** Use only data perceived as most informative:  
**unambiguous data** (Fodor 1998, Lightfoot 1999, Dresher 1999).

**Interpretation Bias:** Use only data that is more accessible (perhaps for language processing reasons) (Lightfoot 1991).

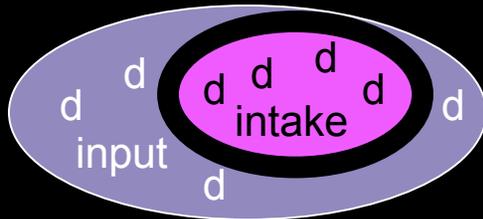
OV unambiguous data:

[...]XP ... Object TensedVerb ...  
...TensedVerb ... Object Verb-Marker ...

VO unambiguous data:

[...]XP [...]XP ... TensedVerb Object ...  
...TensedVerb ... Verb-Marker Object ...

# Modeling Individuals: Learning Biases



**Interpretation Bias:** Use only data perceived as most informative:  
**unambiguous data** (Fodor 1998, Lightfoot 1999, Dresher 1999).

**Interpretation Bias:** Use only structurally simple (degree-0) data (Lightfoot 1991).

OV unambiguous data:

[...]XP ... Object TensedVerb ...  
 ...TensedVerb ... Object Verb-Marker ...

VO unambiguous data:

[...]XP [...]XP ... TensedVerb Object ...  
 ...TensedVerb ... Verb-Marker Object ...

Jack told his mother that the giant was easy to fool.

[----Degree-0-----]

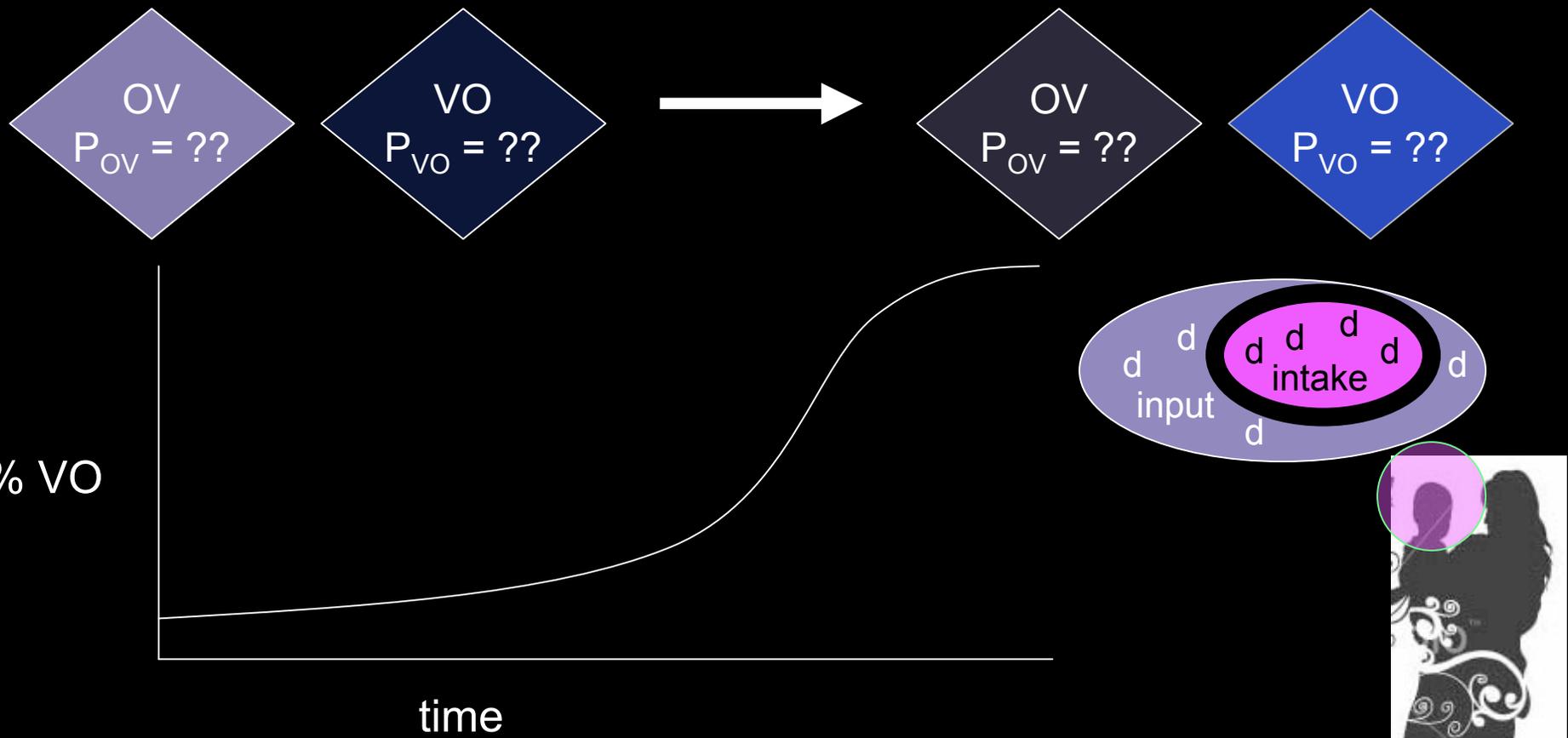
[-----Degree-1-----]

# Modeling Individuals: Learning Biases

**The point of interpretation biases:** Unambiguous degree-0 data distribution may differ the right amount from population's underlying distribution to change at the right rate.

~1000 A.D.-1150 A.D.: OV-biased

~1200 A.D.: VO-biased



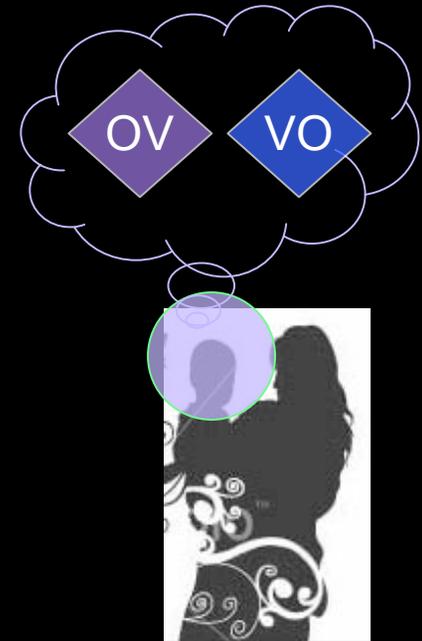
# Modeling Individuals: Knowledge & Learning

Individual learner tracks  $p_{VO}$  = probability of using **VO**  
probability of using **OV** =  $1 - p_{VO}$

Old English:  $0.0 \leq p_{VO} \leq 1.0$

Ex:  $0.3 = 30\%$  **VO**,  $70\%$  **OV** during generation

Initial  $p_{VO} = 0.5$  (unbiased)



# Modeling Individuals: Knowledge & Learning

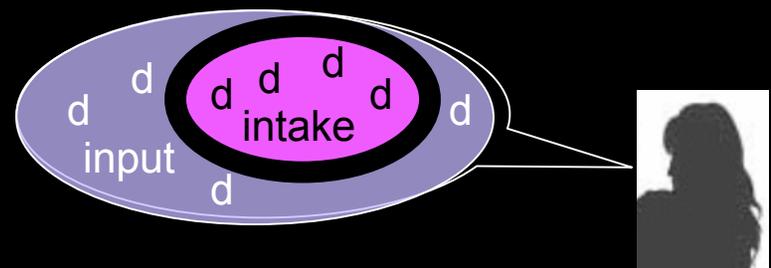
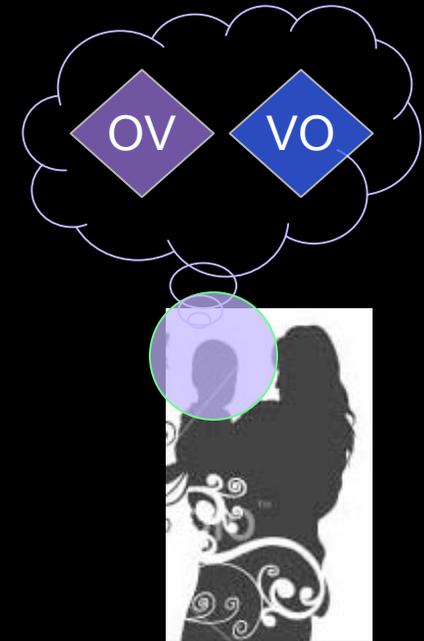
Individual learner tracks  $p_{VO}$  = probability of using **VO**  
probability of using **OV** =  $1 - p_{VO}$

Old English:  $0.0 \leq p_{VO} \leq 1.0$

Ex:  $0.3 = 30\%$  **VO**,  $70\%$  **OV** during generation

Initial  $p_{VO} = 0.5$  (unbiased)

Data from old members of population, filtered through selective learning biases.



# Modeling Individuals: Knowledge & Learning

Individual learner tracks  $p_{VO}$  = probability of using VO  
probability of using OV =  $1 - p_{VO}$

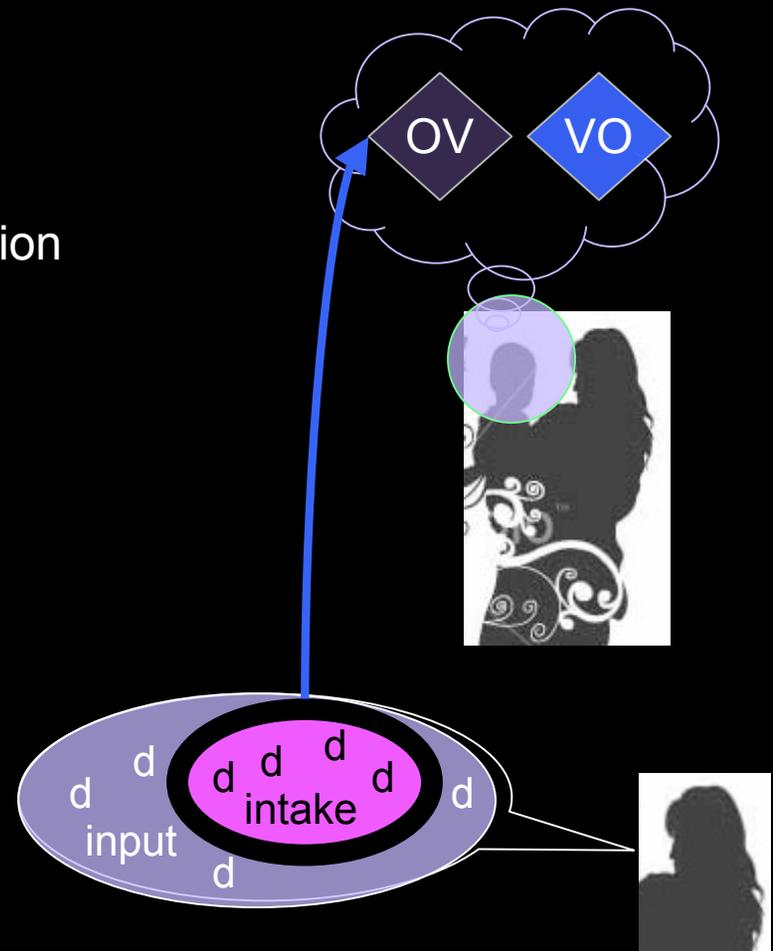
Old English:  $0.0 \leq p_{VO} \leq 1.0$

Ex: 0.3 = 30% VO, 70% OV during generation

Initial  $p_{VO} = 0.5$  (unbiased)

Data from old members of population, filtered through selective learning biases.

Individual update: Bayesian updating for binomial distribution (Chew 1971), adapted



# Zoom-In on Updating Procedure

$$\text{Max}(\text{Prob}(p_{VO} | u)) = \text{Max}\left(\frac{\text{Prob}(u | p_{VO}) * \text{Prob}(p_{VO})}{\text{Prob}(u)}\right)$$

$$\text{Prob}(p_{VO} | u) = \frac{p_{VO} * \binom{n}{r} * p_{VO}^r * (1 - p_{VO})^{n-r}}{\text{Prob}(u)} \quad (\text{for each point } r, 0 \leq r \leq n)$$

$$\frac{d}{dp_{VO}} \left( \frac{p_{VO} * \binom{n}{r} * p_{VO}^r * (1 - p_{VO})^{n-r}}{\text{Prob}(u)} \right) = 0$$

$$\frac{d}{dp_{VO}} \left( \frac{p_{VO} * \binom{n}{r} * p_{VO}^r * (1 - p_{VO})^{n-r}}{\text{Prob}(u)} \right) = 0 \quad (\text{P}(u) \text{ is constant with respect to } p_{VO})$$

$$p_{VO} = \frac{r+1}{n+1}, r = p_{VO_{prev}} * n$$

Replace 1 in numerator and denominator with  $c = p_{VO_{prev}} * m$  if VO,  $c = (1 - p_{VO_{prev}}) * m$  if OV

$$3.0 \leq m \leq 5.0$$

# Zoom-In on Updating Procedure

If **OV** data point

$$p_{VO} = (p_{VO_{prev}} * n) / (n+c)$$

If **VO** data point

$$p_{VO} = (p_{VO_{prev}} * n+c) / (n+c)$$

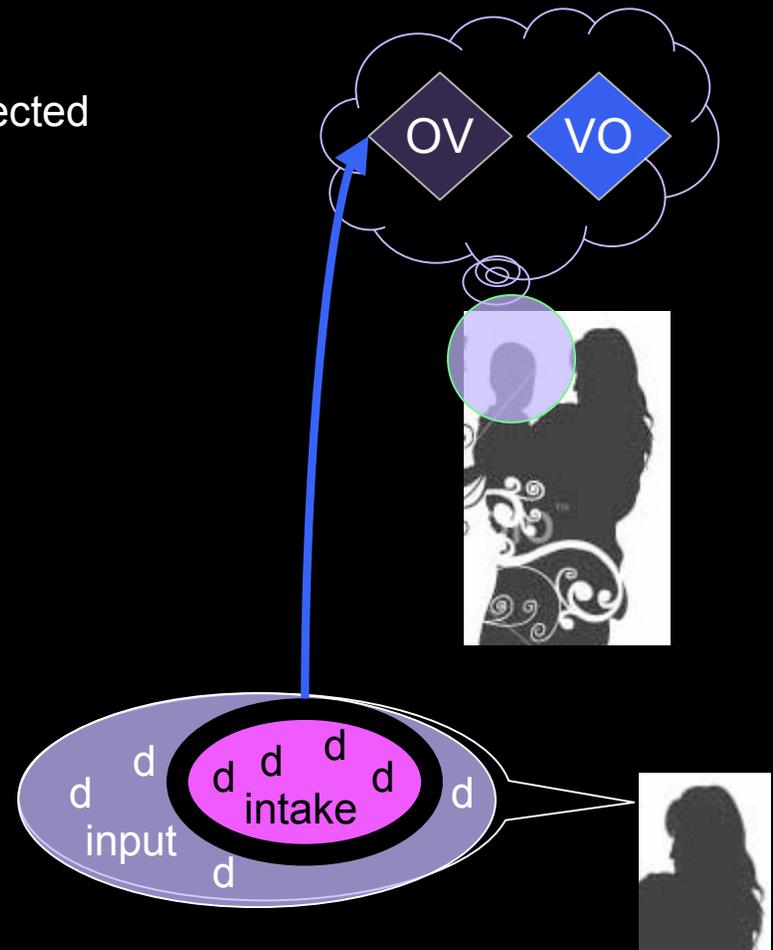
Model parameters:

$c$  represents learner's confidence in data point (calibrated from data)

$n$  represents quantity of intake (2000)

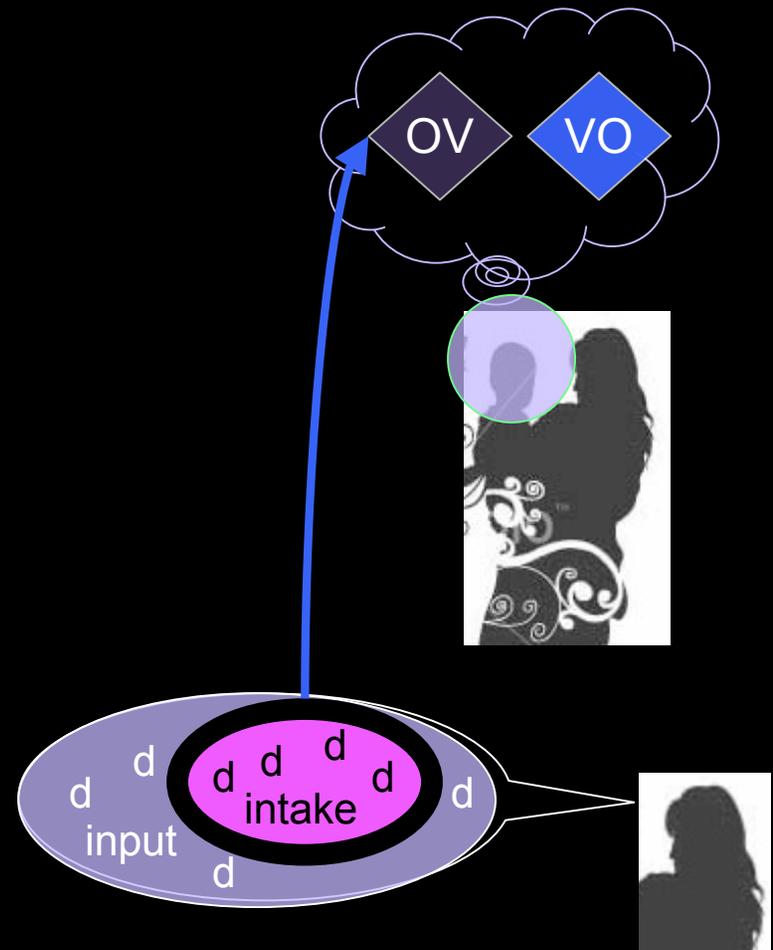
Important: Online update procedure (psychological plausibility, given human memory)

Involves previous probability & expected amount of data in learning period



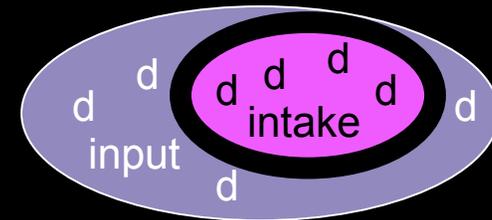
# Individual-Level Learning Algorithm

- (1) Initial  $p_{VO} = 0.5$ .
- (2) Encounter data point from an average member of the population.
- (3) If the data point is degree-0 and unambiguous, use update functions to shift hypothesis probabilities.
- (4) Repeat (2-3) until the learning period is over, as determined by  $n$ .



# Biased Data Intake Distributions in Old English

$p_{VO}$  shifts away from 0.5 when there is more of one data type in the intake than the other (**advantage** (Yang 2000) of one data type).

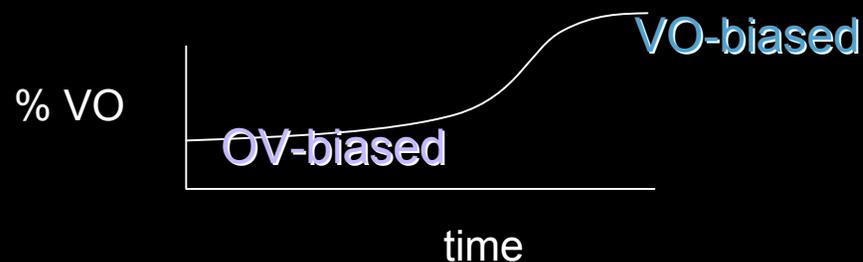


So the bias in the degree-0 unambiguous data distribution controls an individual's final  $p_{VO}$  in this model.

	OV Advantage in Unamb D0
1000 A.D.	19.5%
1000-1150 A.D.	2.8%
1200 A.D.	-2.7%

OV-biased

VO-biased

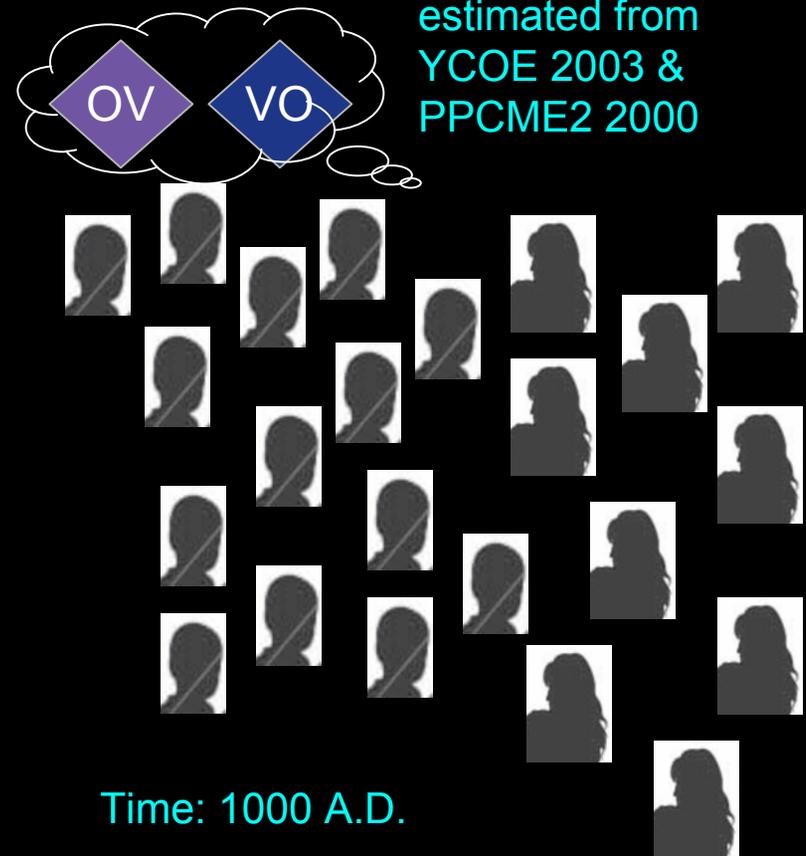


# Population-Level Model

- (1) Set the age range of the population from 0 to 60 years old and create 18,000 population members.
- (2) Initialize the members of the population to the average  $p_{VO}$  at 1000 A.D. Set the time to 1000 A.D.

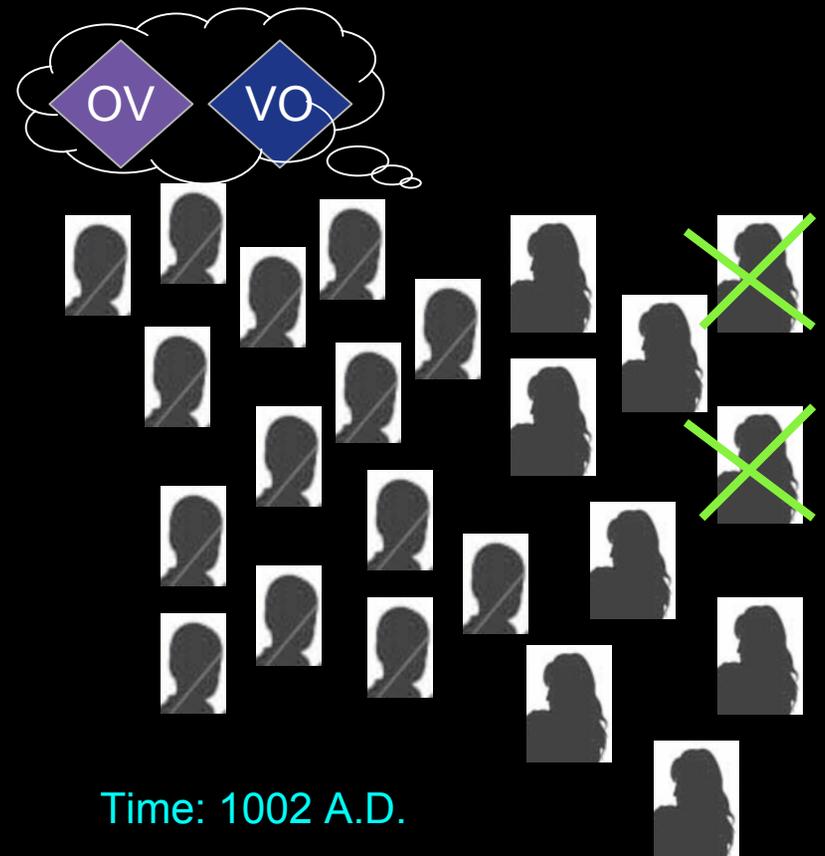
Population size estimated from population statistics of the time period (Koenigsberger & Briggs 1987)

Average  $p_{VO}$  estimated from YCOE 2003 & PPCME2 2000



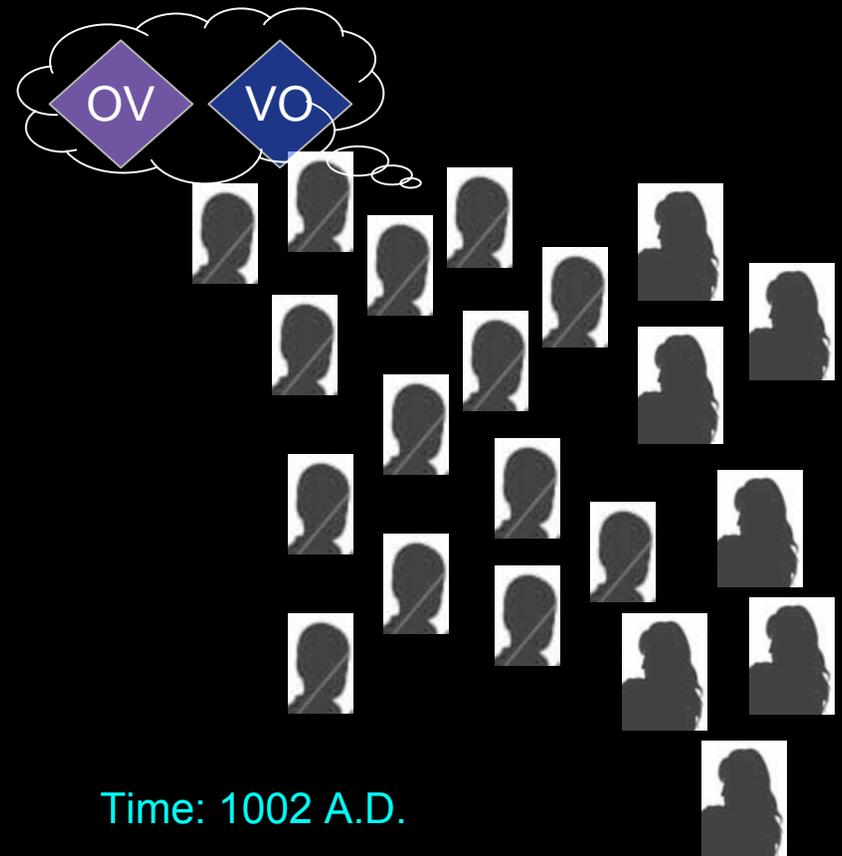
# Population-Level Model

- (1) Set the age range of the population from 0 to 60 years old and create 18,000 population members.
- (2) Initialize the members of the population to the average  $p_{VO}$  at 1000 A.D. Set the time to 1000 A.D.
- (3) Move forward 2 years.
- (4) Members age 59-60 die off.



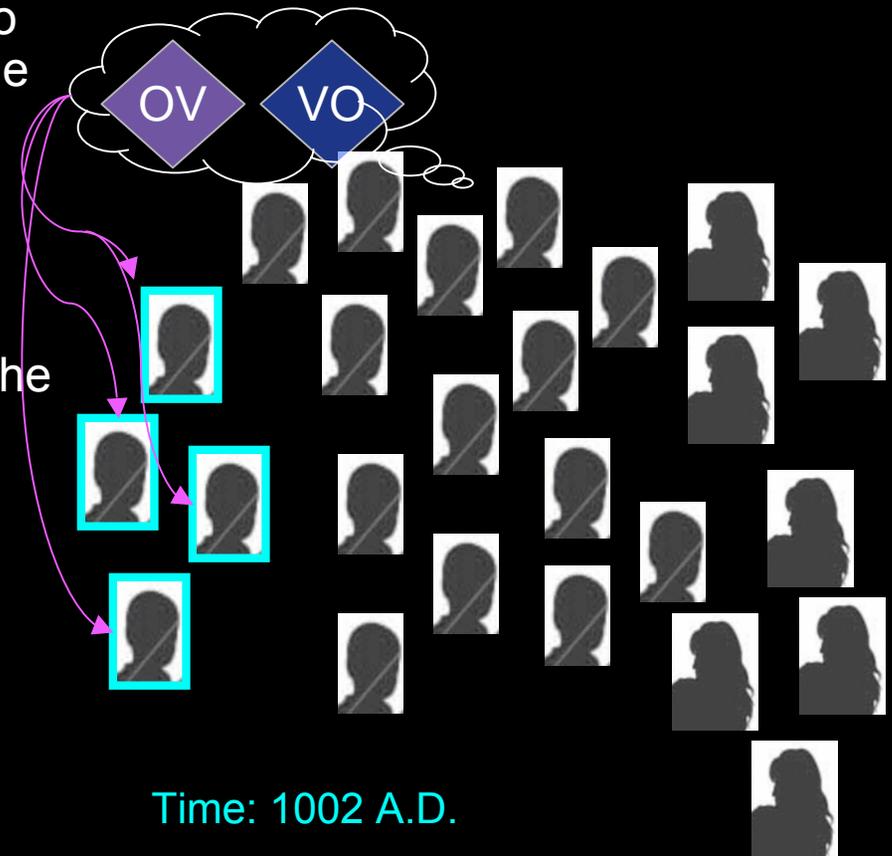
# Population-Level Model

- (1) Set the age range of the population from 0 to 60 years old and create 18,000 population members.
- (2) Initialize the members of the population to the average  $p_{VO}$  at 1000 A.D. Set the time to 1000 A.D.
- (3) Move forward 2 years.
- (4) Members age 59-60 die off. The rest of the population ages 2 years.



# Population-Level Model

- (1) Set the age range of the population from 0 to 60 years old and create 18,000 population members.
- (2) Initialize the members of the population to the average  $p_{VO}$  at 1000 A.D. Set the time to 1000 A.D.
- (3) Move forward 2 years.
- (4) Members age 59-60 die off. The rest of the population ages 2 years.
- (5) New members are born. These new members use the individual acquisition algorithm to set their  $p_{VO}$ .

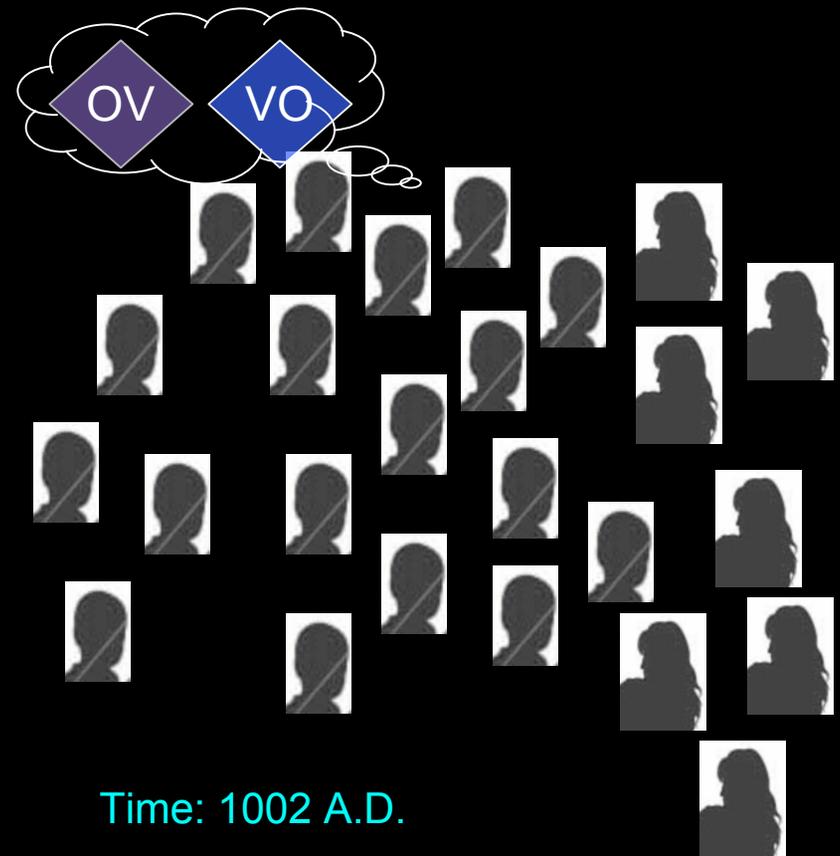


Population growth rate  
estimated from population  
statistics of the time period  
(Koenigsberger & Briggs 1987)

Time: 1002 A.D.

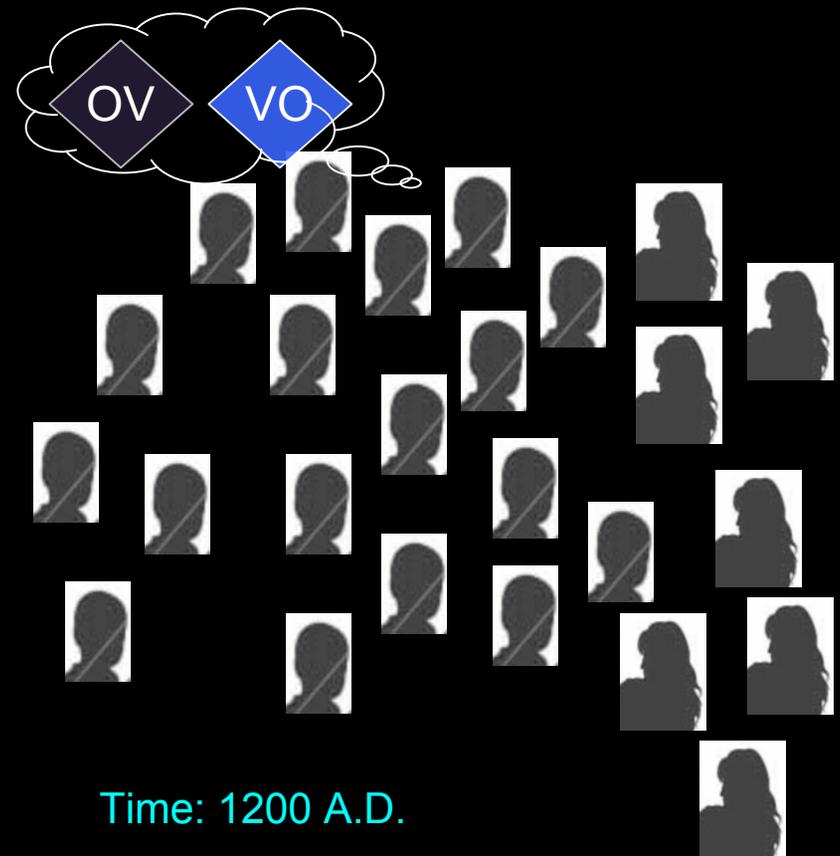
# Population-Level Model

- (1) Set the age range of the population from 0 to 60 years old and create 18,000 population members.
- (2) Initialize the members of the population to the average  $p_{VO}$  at 1000 A.D. Set the time to 1000 A.D.
- (3) Move forward 2 years.
- (4) Members age 59-60 die off. The rest of the population ages 2 years.
- (5) New members are born. These new members use the individual acquisition algorithm to set their  $p_{VO}$ .



# Population-Level Model

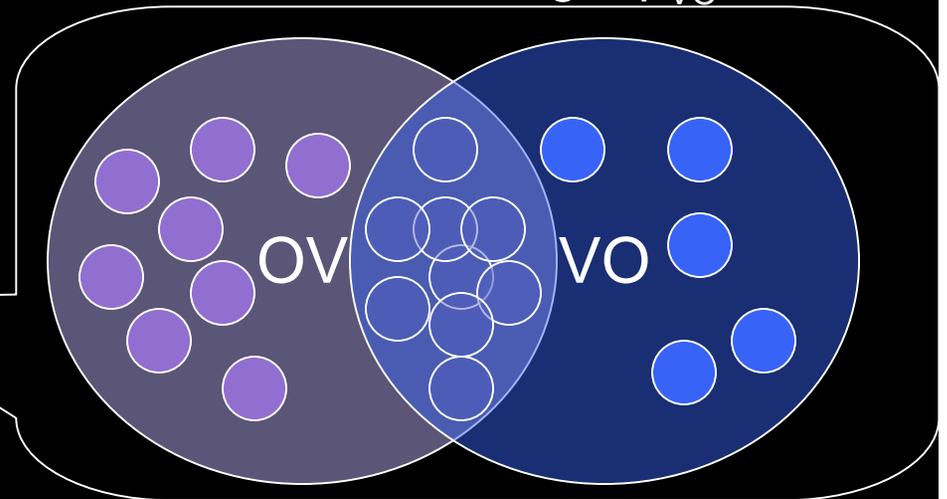
- (1) Set the age range of the population from 0 to 60 years old and create 18,000 population members.
- (2) Initialize the members of the population to the average  $p_{VO}$  at 1000 A.D. Set the time to 1000 A.D.
- (3) Move forward 2 years.
- (4) Members age 59-60 die off. The rest of the population ages 2 years.
- (5) New members are born. These new members use the individual acquisition algorithm to set their  $p_{VO}$ .
- (6) Repeat steps (3-5) until the year 1200 A.D.



# Empirical Grounding Issues: What exactly is the underlying distribution?

Historical data used to initialize population's  $p_{VO}$  at 1000 A.D., calibrate population's  $p_{VO}$  between 1000 and 1150 A.D., and check target  $p_{VO}$  at 1200 A.D.

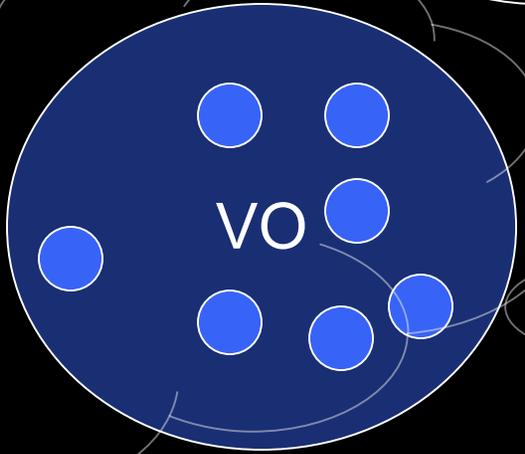
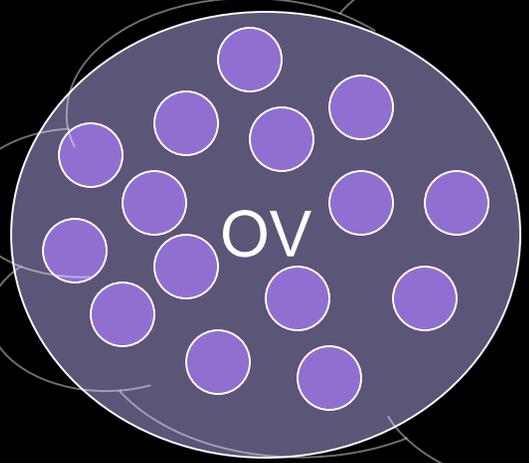
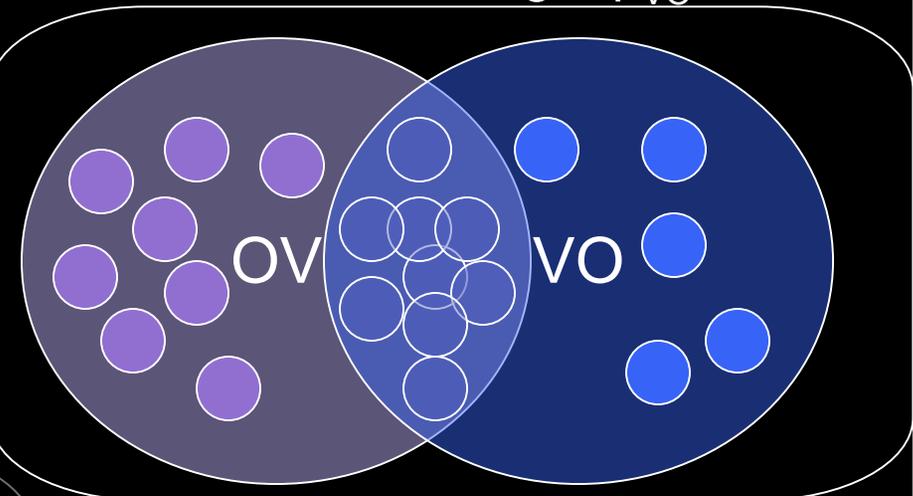
Historical data distributions: some data are ambiguous



# Empirical Grounding Issues: What exactly is the underlying distribution?

Historical data used to initialize population's  $p_{VO}$  at 1000 A.D., calibrate population's  $p_{VO}$  between 1000 and 1150 A.D., and check target  $p_{VO}$  at 1200 A.D.

Historical data distributions: some data are ambiguous



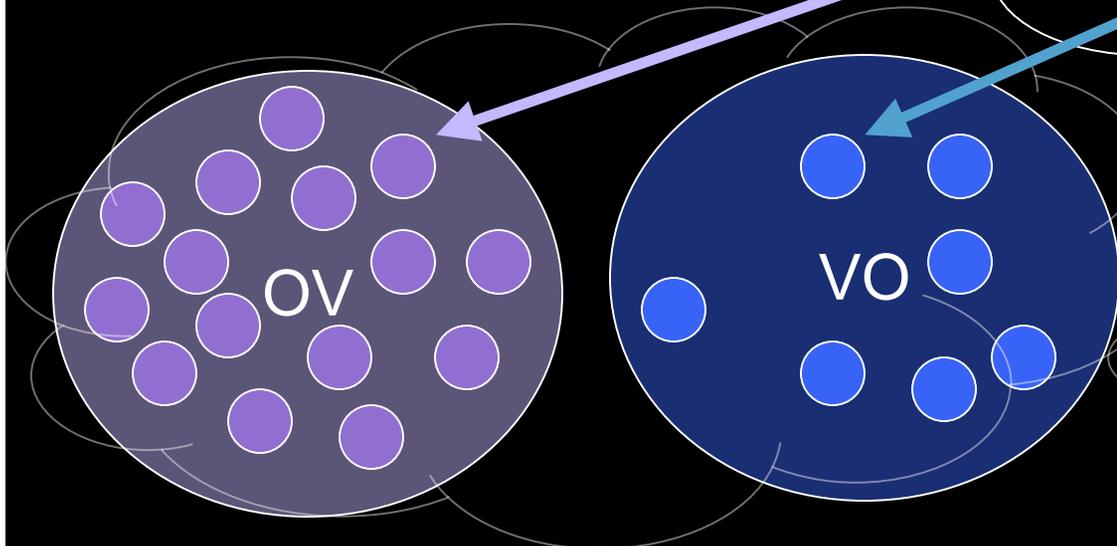
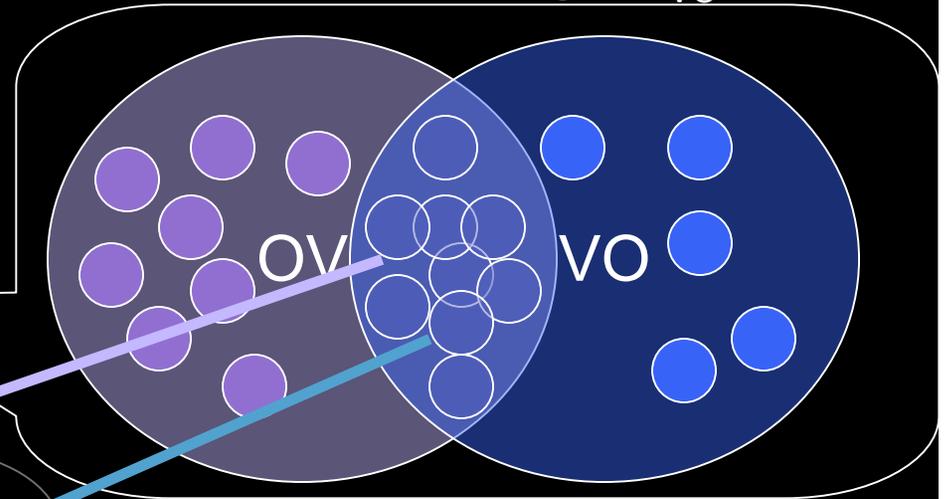
$p_{VO}$ : underlying distribution is not ambiguous



# Empirical Grounding Issues: What exactly is the underlying distribution?

Historical data used to initialize population's  $p_{VO}$  at 1000 A.D., calibrate population's  $p_{VO}$  between 1000 and 1150 A.D., and check target  $p_{VO}$  at 1200 A.D.

Historical data distributions: some data are ambiguous



$p_{VO}$ : underlying distribution is not ambiguous

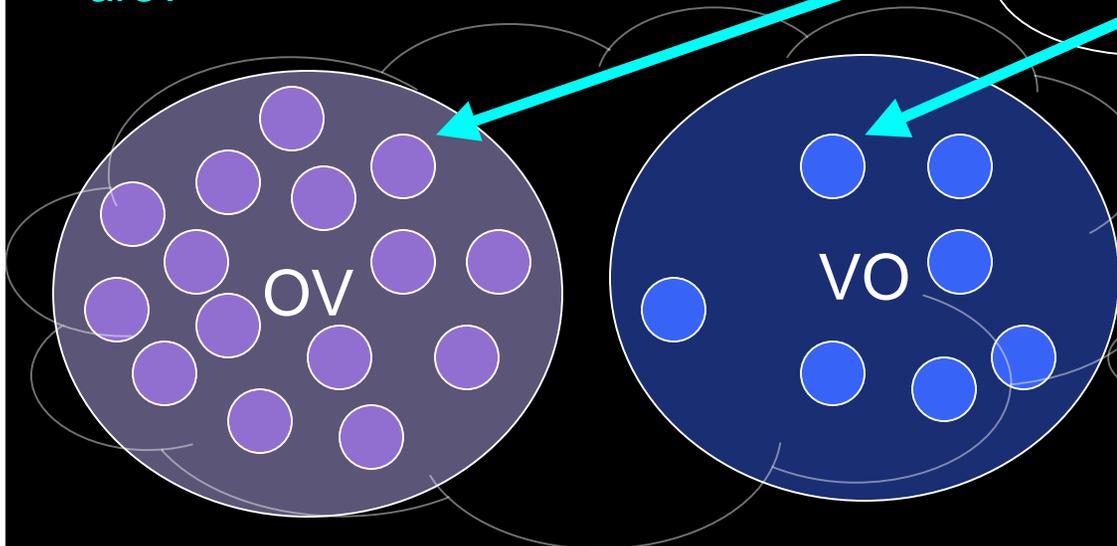
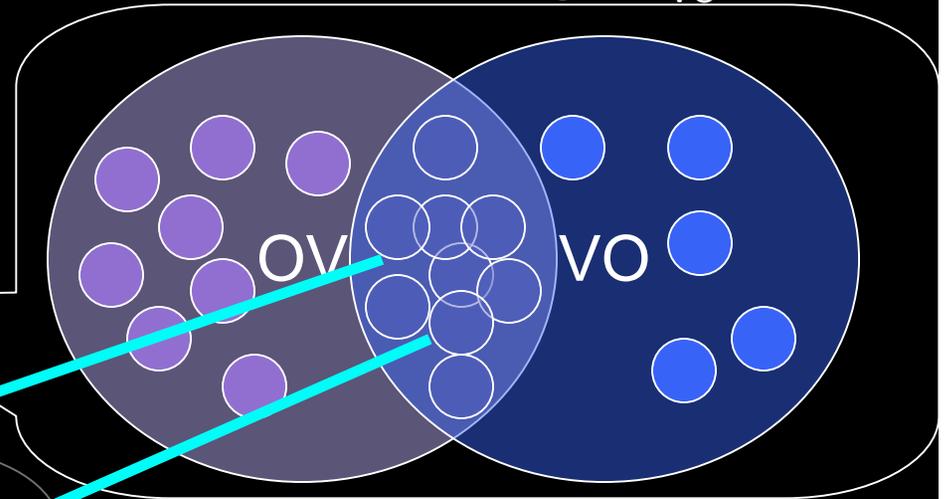


# Empirical Grounding Issues: What exactly is the underlying distribution?

Historical data used to initialize population's  $p_{VO}$  at 1000 A.D., calibrate population's  $p_{VO}$  between 1000 and 1150 A.D., and check target  $p_{VO}$  at 1200 A.D.

Historical data distributions: some data are ambiguous

How do we figure out what the ambiguous data are?



$p_{VO}$ : underlying distribution is not ambiguous



# Empirical Grounding Issues: What exactly is the underlying distribution?

(YCOE and PPCME2 Corpora)

% Ambiguous Utterances

	Degree-0 % Ambiguous	Degree-1 % Ambiguous
1000 A.D.	76%	28%
1000 - 1150 A.D.	80%	25%
1200 A.D.	71%	10%

Observations:

(1) Degree-1 data less ambiguous than degree-0 data.

# Empirical Grounding Issues: What exactly is the underlying distribution?

(YCOE and PPCME2 Corpora)

% Advantage

	OV Advantage in Unamb <b>D0</b>	OV Advantage in Unamb <b>D1</b>
1000 A.D.	19.5%	41.7%
1000-1150 A.D.	2.8%	28.7%
1200 A.D.	-2.7%	-45.2%

Observations:

- (1) Degree-1 data less ambiguous than degree-0 data.
- (2) Advantage is magnified in degree-1.

# Empirical Grounding Issues:

## What exactly is the underlying distribution?

Observations:

- (1) Degree-1 data less ambiguous than degree-0 data.
- (2) Advantage is magnified in degree-1.

Assumption: Ambiguous data distorts underlying distribution.

Assumption: degree-1 distribution less distorted from underlying distribution.

# Empirical Grounding Issues: What exactly is the underlying distribution?

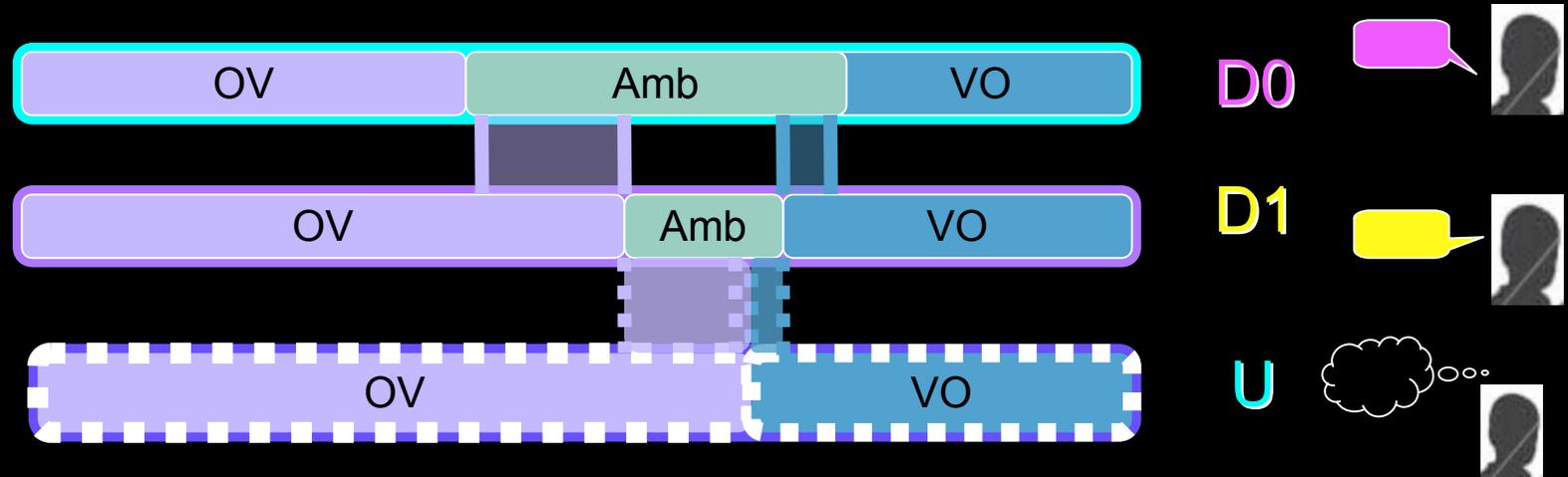
Observations:

- (1) Degree-1 data less ambiguous than degree-0 data.
- (2) Advantage is magnified in degree-1.

Assumption: Ambiguous data distorts underlying distribution.

Assumption: degree-1 distribution less distorted from underlying distribution.

Plan of Action: Use the difference in distortion between the **degree-0** and **degree-1** unambiguous data distributions to estimate the difference in distortion between the **degree-1** distribution and the **underlying** unambiguous data distribution in a speaker's mind.



# Empirical Grounding Issues: What exactly is the underlying distribution?

Observations:

- (1) Degree-1 data less ambiguous than degree-0 data.
- (2) Advantage is magnified in degree-1.

Assumption: Ambiguous data distorts underlying distribution

Assumption: degree-1 distribution less distorted from underlying distribution.

$$\frac{\gamma * d0 - u1d1'}{\gamma * d0} = Ld1tod0 * \frac{ad1' - (\gamma * d0 - u1d1')}{u2d1' + ad1' - (\gamma * d0 - u1d1')}$$

$\gamma$  = underlying pvo

known quantities

$d0$  = total degree -0 data,  $d1$  = total degree -1 data

$u1d1'$  = normalized unambiguous OV degree -1 data

$u2d1'$  = normalized unambiguous VO degree -1 data

$Ld1tod0$  = loss ratio (OV/VO) from degree -1 to degree -0 distribution

$ad1'$  = normalized ambiguous degree -1 data

$$\gamma = \frac{-(d0)(d0 + u1d1' - Ld1tod0*(ad1' + u1d1'))}{2(Ld1tod0 + 1)(d0^2)}$$

$$+/- \frac{\sqrt{((d0)(d0 + u1d1' - Ld1tod0*(ad1' + u1d1')))^2 - 4(Ld1tod0 + 1)(d0^2)((-1)(d0 * u1d1'))}}{2(Ld1tod0 + 1)(d0^2)}$$

derived quantities

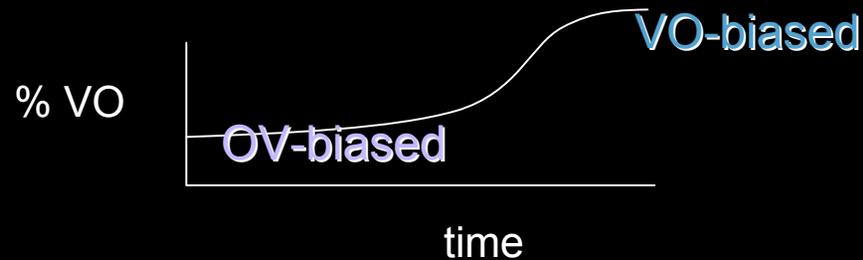
# Empirical Grounding Issues: What exactly is the underlying distribution?

Observations:

- (1) Degree-1 data less ambiguous than degree-0 data.
- (2) Advantage is magnified in degree-1.

Assumption: Ambiguous data distorts underlying distribution

Assumption: degree-1 distribution less distorted from underlying distribution.



	(Initialization) 1000 A.D.	(Calibration) 1000-1150 A.D.	(Termination) 1200 A.D.
Average $p_{VO}$	0.234	0.310	0.747

OV-biased

VO-biased

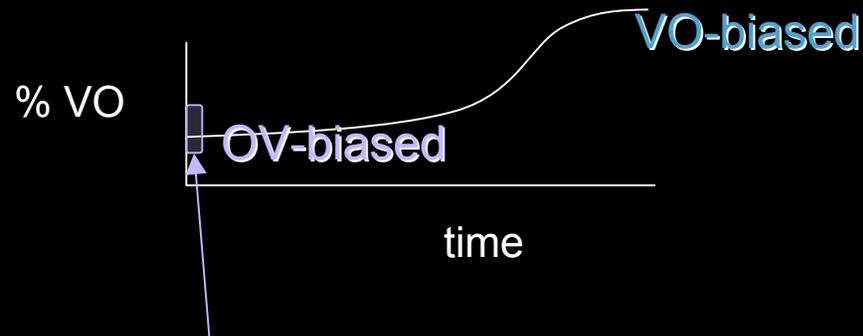
# Empirical Grounding Issues: What exactly is the underlying distribution?

Observations:

- (1) Degree-1 data less ambiguous than degree-0 data.
- (2) Advantage is magnified in degree-1.

Assumption: Ambiguous data distorts underlying distribution

Assumption: degree-1 distribution less distorted from underlying distribution.



	(Initialization) 1000 A.D.	(Calibration) 1000-1150 A.D.	(Termination) 1200 A.D.
Average $p_{VO}$	0.234	0.310	0.747

OV-biased

VO-biased

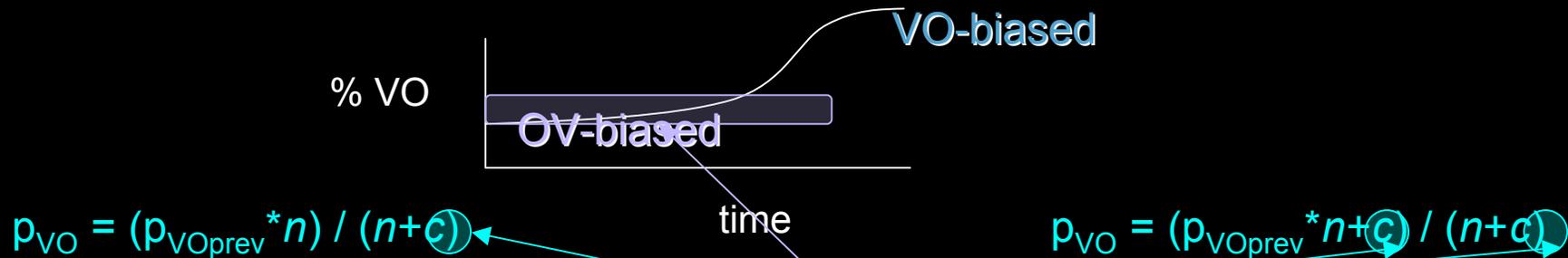
# Empirical Grounding Issues: What exactly is the underlying distribution?

Observations:

- (1) Degree-1 data less ambiguous than degree-0 data.
- (2) Advantage is magnified in degree-1.

Assumption: Ambiguous data distorts underlying distribution

Assumption: degree-1 distribution less distorted from underlying distribution.



	(Initialization) 1000 A.D.	(Calibration) 1000-1150 A.D.	(Termination) 1200 A.D.
Average $p_{VO}$	0.234	0.310	0.747

OV-biased

VO-biased

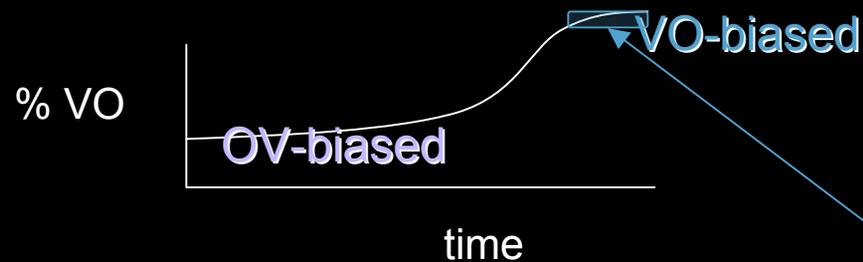
# Empirical Grounding Issues: What exactly is the underlying distribution?

Observations:

- (1) Degree-1 data less ambiguous than degree-0 data.
- (2) Advantage is magnified in degree-1.

Assumption: Ambiguous data distorts underlying distribution

Assumption: degree-1 distribution less distorted from underlying distribution.

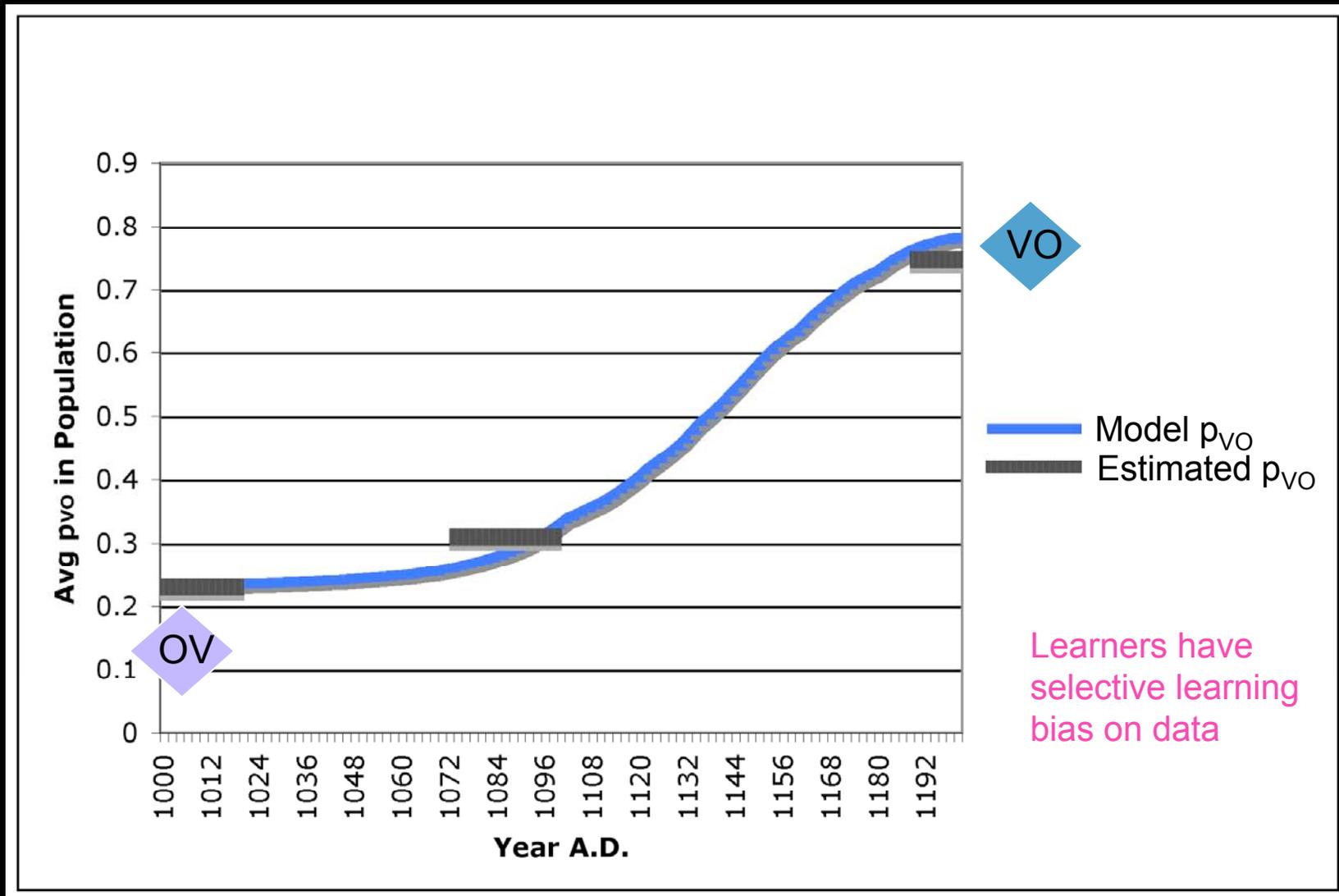


	(Initialization) 1000 A.D.	(Calibration) 1000-1150 A.D.	(Termination) 1200 A.D.
Average $p_{VO}$	0.234	0.310	0.747

OV-biased

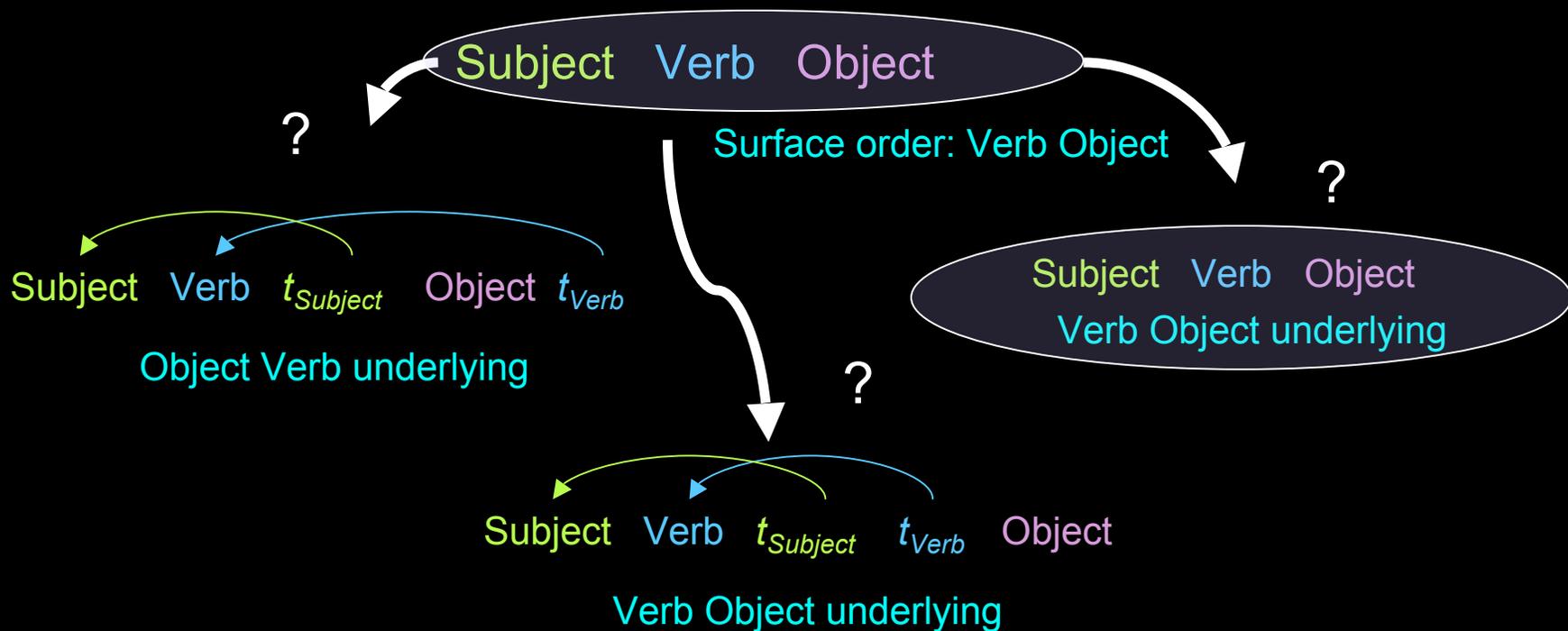
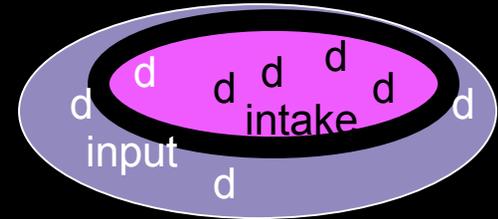
VO-biased

# Linguistic Evolution: Change at the Historically-Attested Rate



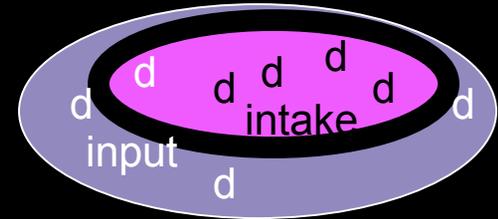
# Linguistic Evolution: Different Individual-Level Learning

Learner uses ambiguous data. Strategy for learning:  
assume surface order is actual order. (Fodor 1998)



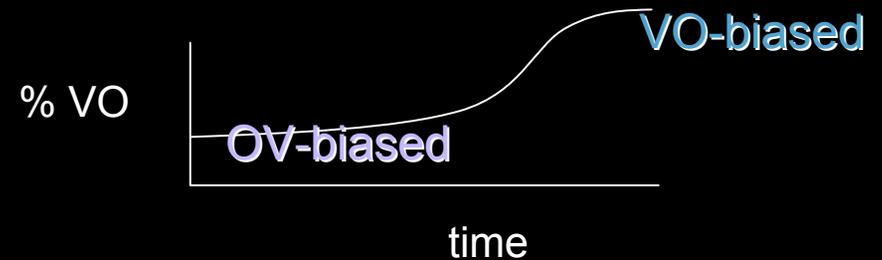
# Linguistic Evolution: Different Individual-Level Learning

Learner uses ambiguous data. Strategy for learning:  
assume surface order is actual order. (Fodor 1998)



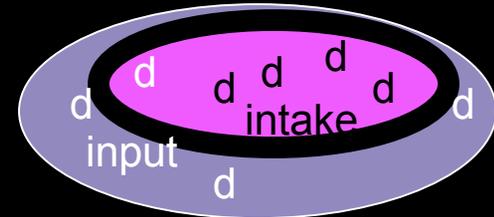
Advantage in intake determines learner's ending  
distribution between OV and VO order.

Need this trajectory



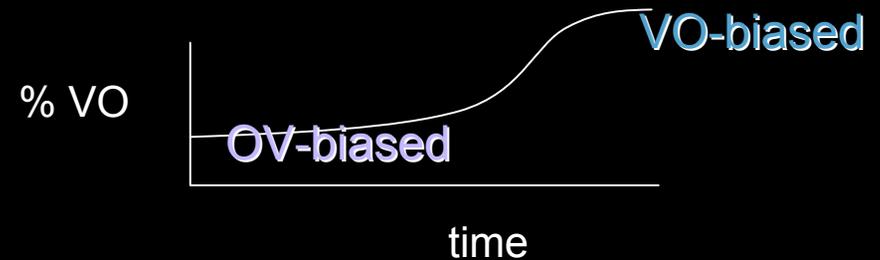
# Linguistic Evolution: Different Individual-Level Learning

Learner uses ambiguous data. Strategy for learning:  
assume surface order is actual order. (Fodor 1998)



Advantage in intake determines learner's ending  
distribution between OV and VO order.

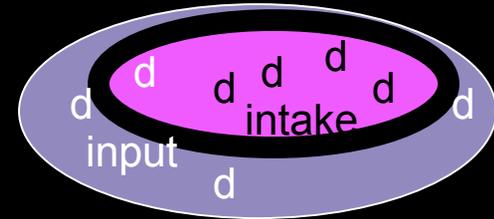
Need this trajectory



	Degree-0 OV Advantage
1000 A.D.	-21.0%
1000 - 1150 A.D.	-26.9%
1200 A.D.	-21.8%

# Linguistic Evolution: Different Individual-Level Learning

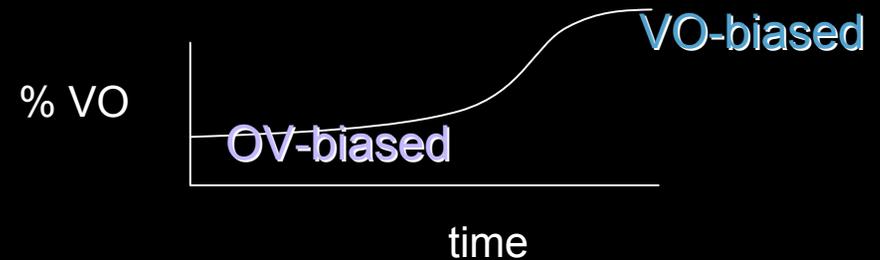
Learner uses ambiguous data. Strategy for learning: assume surface order is actual order. (Fodor 1998)



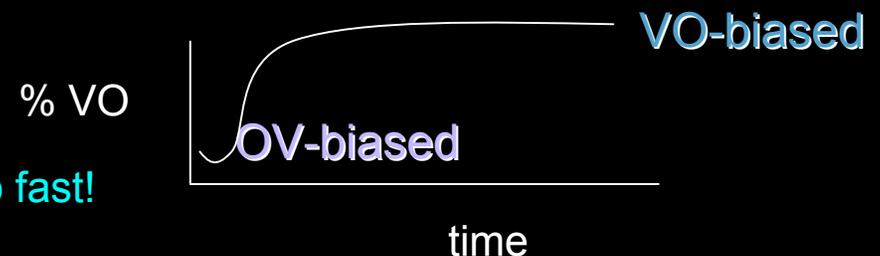
Advantage in intake determines learner's ending distribution between OV and VO order.

Need this trajectory

	Degree-0 OV Advantage
1000 A.D.	-21.0%
1000 - 1150 A.D.	-26.9%
1200 A.D.	-21.8%



Problem: VO-biased all the way through, even at 1000 A.D.



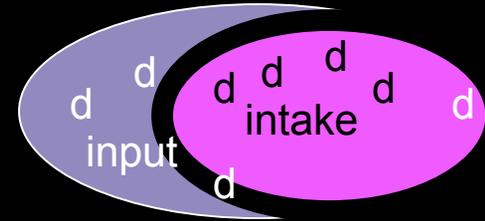
Change is too fast!

# Linguistic Evolution: Different Individual-Level Learning

Learner uses degree-0 and degree-1 unambiguous data.

(YCOE and PPCME2 Corpora)

% Advantage

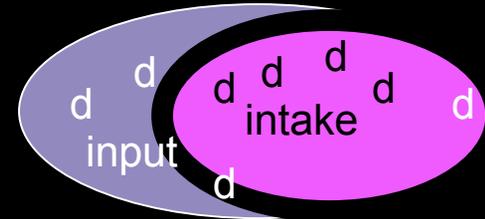


	OV Advantage in Unamb <b>D0</b>	OV Advantage in Unamb <b>D1</b>
1000 A.D.	19.5%	41.7%
1000-1150 A.D.	2.8%	28.7%
1200 A.D.	-2.7%	-45.2%

Very strongly OV-  
biased before  
1150 A.D.

# Linguistic Evolution: Different Individual-Level Learning

Learner uses degree-0 and degree-1 unambiguous data.



(YCOE and PPCME2 Corpora)

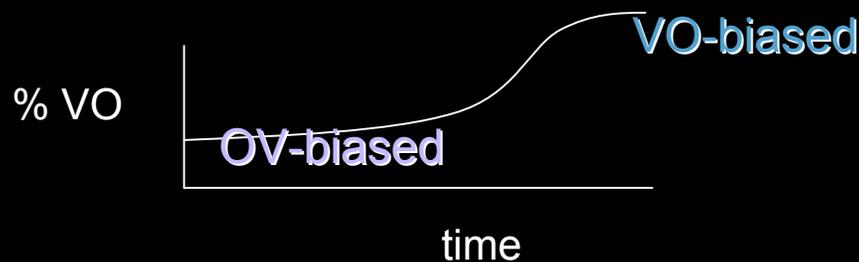
% Advantage

	OV Advantage in Unamb <b>D0</b>	OV Advantage in Unamb <b>D1</b>
1000 A.D.	19.5%	41.7%
1000-1150 A.D.	2.8%	28.7%
1200 A.D.	-2.7%	-45.2%

Very strongly OV-biased before 1150 A.D.

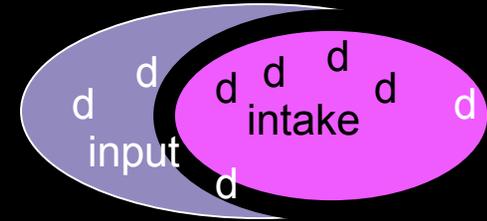
Need this trajectory

But population must become VO-biased.



# Linguistic Evolution: Different Individual-Level Learning

Learner uses degree-0 and degree-1 unambiguous data.



(YCOE and PPCME2 Corpora)

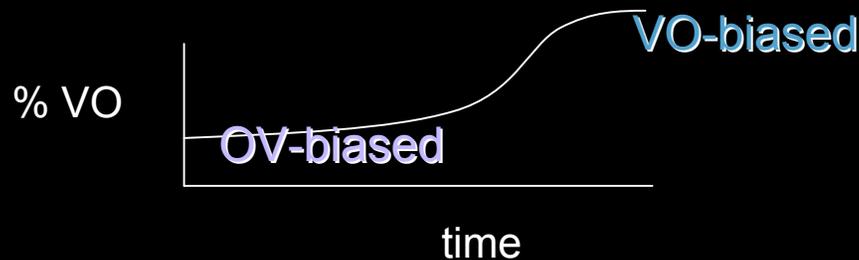
% Advantage

	OV Advantage in Unamb <b>D0</b>	OV Advantage in Unamb <b>D1</b>
1000 A.D.	19.5%	41.7%
1000-1150 A.D.	2.8%	28.7%
1200 A.D.	-2.7%	-45.2%

Very strongly OV-biased before 1150 A.D.

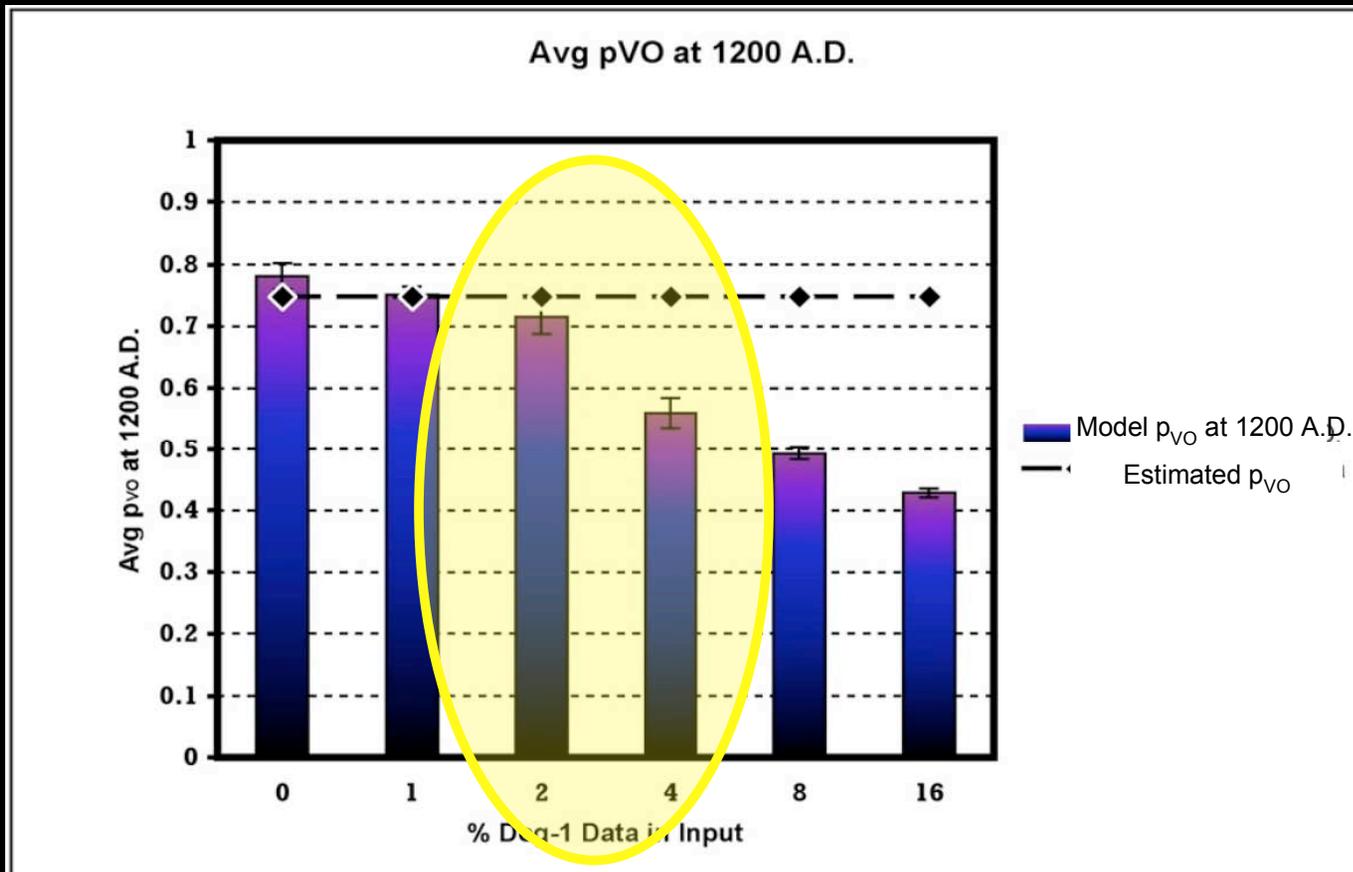
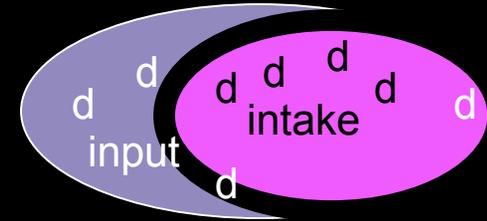
Need this trajectory

Can a population learning from degree-1 data make the change to VO-biased?



# Linguistic Evolution: Different Individual-Level Learning

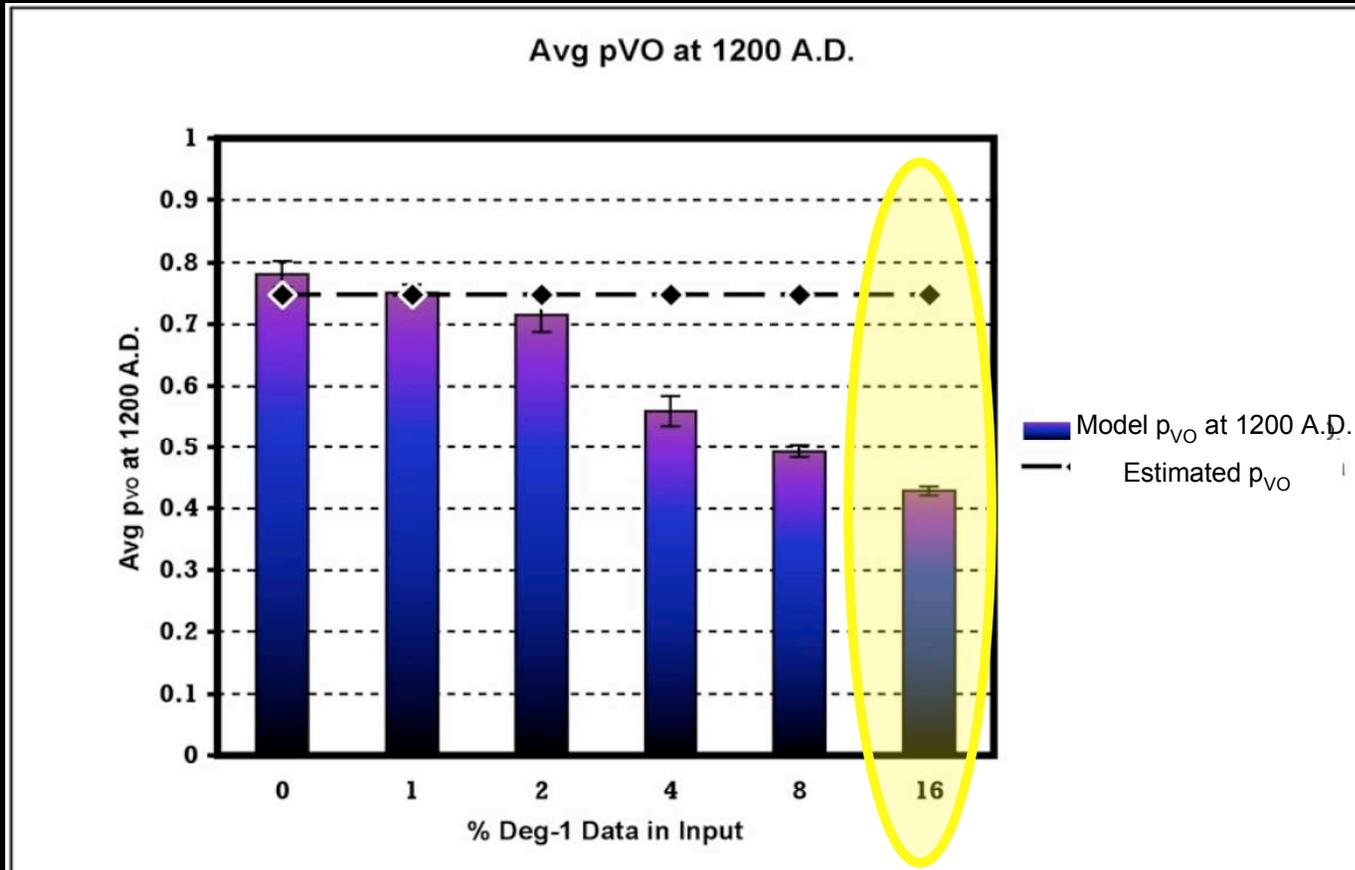
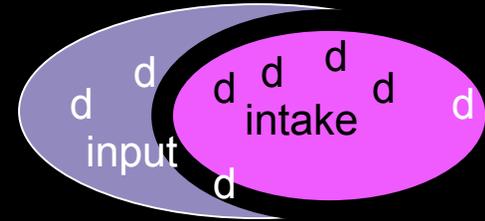
Learner uses degree-0 and degree-1 unambiguous data.



Modeled population can change at the right rate only if input contains less than 4% degree-1 data - otherwise, change is too slow for learners not using a degree-0 bias.

# Linguistic Evolution: Different Individual-Level Learning

Learner uses degree-0 and degree-1 unambiguous data.



Estimates from modern English child-directed speech: Input consists of ~16% degree-1 data.

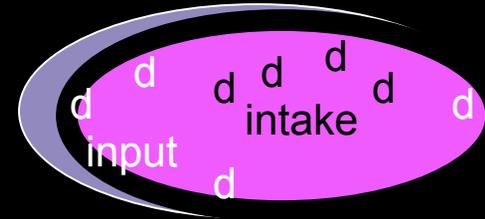
Prognosis: Change would be too slow without a degree-0 bias for individual learners.

# Linguistic Evolution: Different Individual-Level Learning

Learner uses degree-0 and degree-1 data, and learns from ambiguous data.

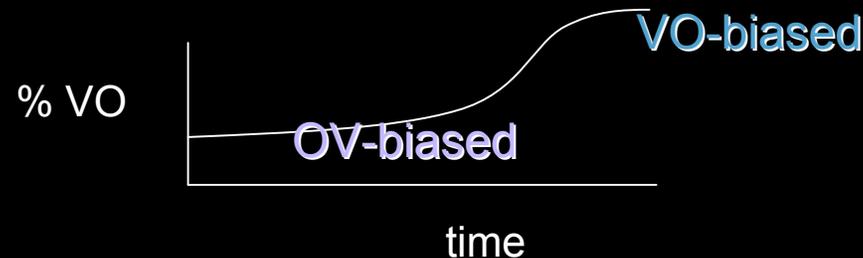
(YCOE and PPCME2 Corpora)

% Advantage



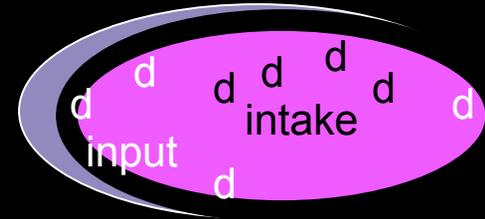
	OV Advantage in D0	OV Advantage in D1
1000 A.D.	-21.0%	28.1%

Need this trajectory



# Linguistic Evolution: Different Individual-Level Learning

Learner uses degree-0 and degree-1 data, and learns from ambiguous data.



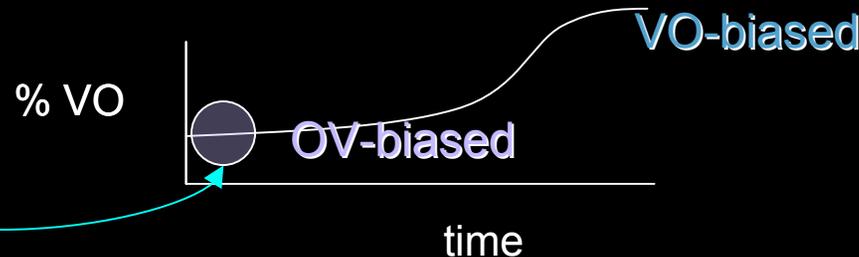
(YCOE and PPCME2 Corpora)

% Advantage

	OV Advantage in D0	OV Advantage in D1
1000 A.D.	-21.0%	28.1%

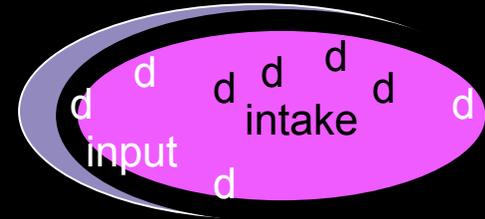
Need this trajectory

Population must remain OV-biased at 1000 A.D.



# Linguistic Evolution: Different Individual-Level Learning

Learner uses degree-0 and degree-1 data, and learns from ambiguous data.



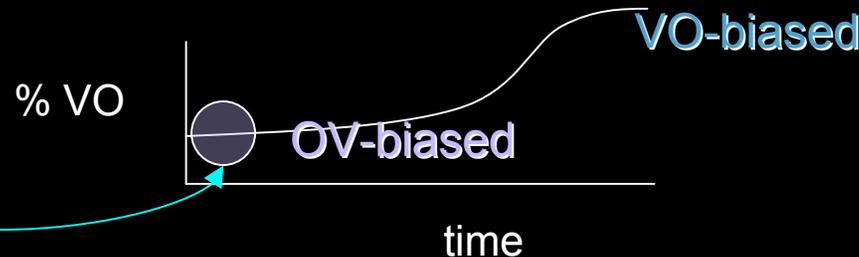
(YCOE and PPCME2 Corpora)

% Advantage

	OV Advantage in D0	OV Advantage in D1
1000 A.D.	-21.0%	28.1%

Need this trajectory

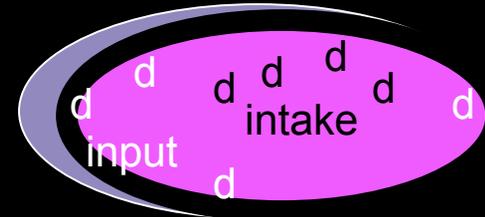
Population must remain OV-biased at 1000 A.D.



To do this, advantage in intake must be for OV order at 1000 A.D. Otherwise, population changes too quickly to VO-biased distribution.

# Linguistic Evolution: Different Individual-Level Learning

Learner uses degree-0 and degree-1 data, and learns from ambiguous data.



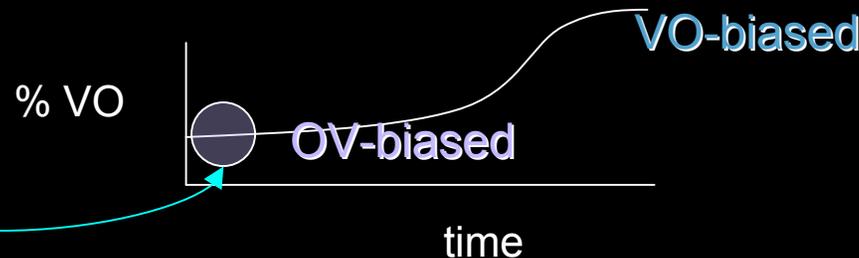
(YCOE and PPCME2 Corpora)

% Advantage

	OV Advantage in D0	OV Advantage in D1
1000 A.D.	-21.0%	28.1%

Need this trajectory

Population must remain OV-biased at 1000 A.D.



Requirement for OV advantage at 1000 A.D.: 43% of input is degree-1 data

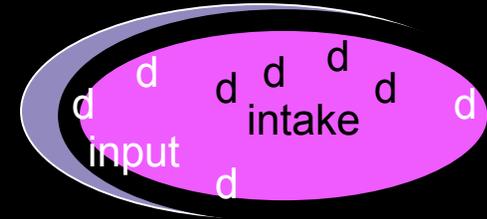
# Linguistic Evolution: Different Individual-Level Learning

Learner uses degree-0 and degree-1 data, and learns from ambiguous data.

(YCOE and PPCME2 Corpora)

% Advantage

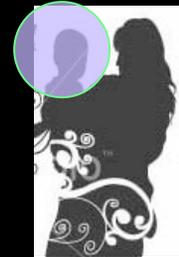
	OV Advantage in D0	OV Advantage in D1
1000 A.D.	-21.0%	28.1%



Requirement for OV advantage at 1000 A.D.: 43% of input is degree-1 data  
...but estimates show only ~16% of it is. Change will be too fast.

# Linguistic Evolution: Summary

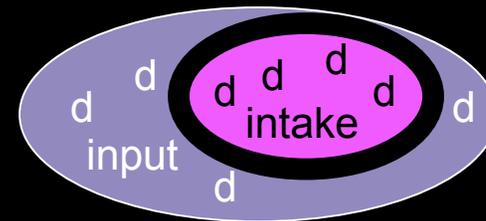
Some cases where linguistic evolution is driven by individual-level learning. Suggested example: Old English word order.



Individual-level learning: can involve selective learning biases, with strong effects on rate of linguistic change within a population.

**Individual-Level Selective Learning:**

- (1) unambiguous data
- (2) degree-0 data



Additional point: linguistic evolution can inform us about the nature of individual learning.

# Linguistic Evolution: Open Questions

(1) If we add complexity to the population model, do we still need these individual-level selective learning biases?

**Weight data points in individual intake using various factors:**

(a) **spatial location of speaker** with respect to learner

(b) **social status of speaker**

(c) **speaker's relation to learner** (family, friend, stranger)

(d) **context of data point** (social context, linguistic context)

(2) Are these learning biases necessary if we look at other language changes where individual-level learning is thought to be the main factor driving change at the population-level?

# Learning-Driven Linguistic Evolution: Take-Home Messages

- (1) Correct population-level behavior can result from correct individual-level learning behavior in some cases (small discrepancies compounded over time).

# Learning-Driven Linguistic Evolution: Take-Home Messages

- (1) Correct population-level behavior can result from correct individual-level learning behavior in some cases (small discrepancies compounded over time).
- (2) In the case study examined here, linguistic evolution occurs at the correct rate only when learners employ selective learning biases that cause them to use only a subset of the available data.

# Learning-Driven Linguistic Evolution: Take-Home Messages

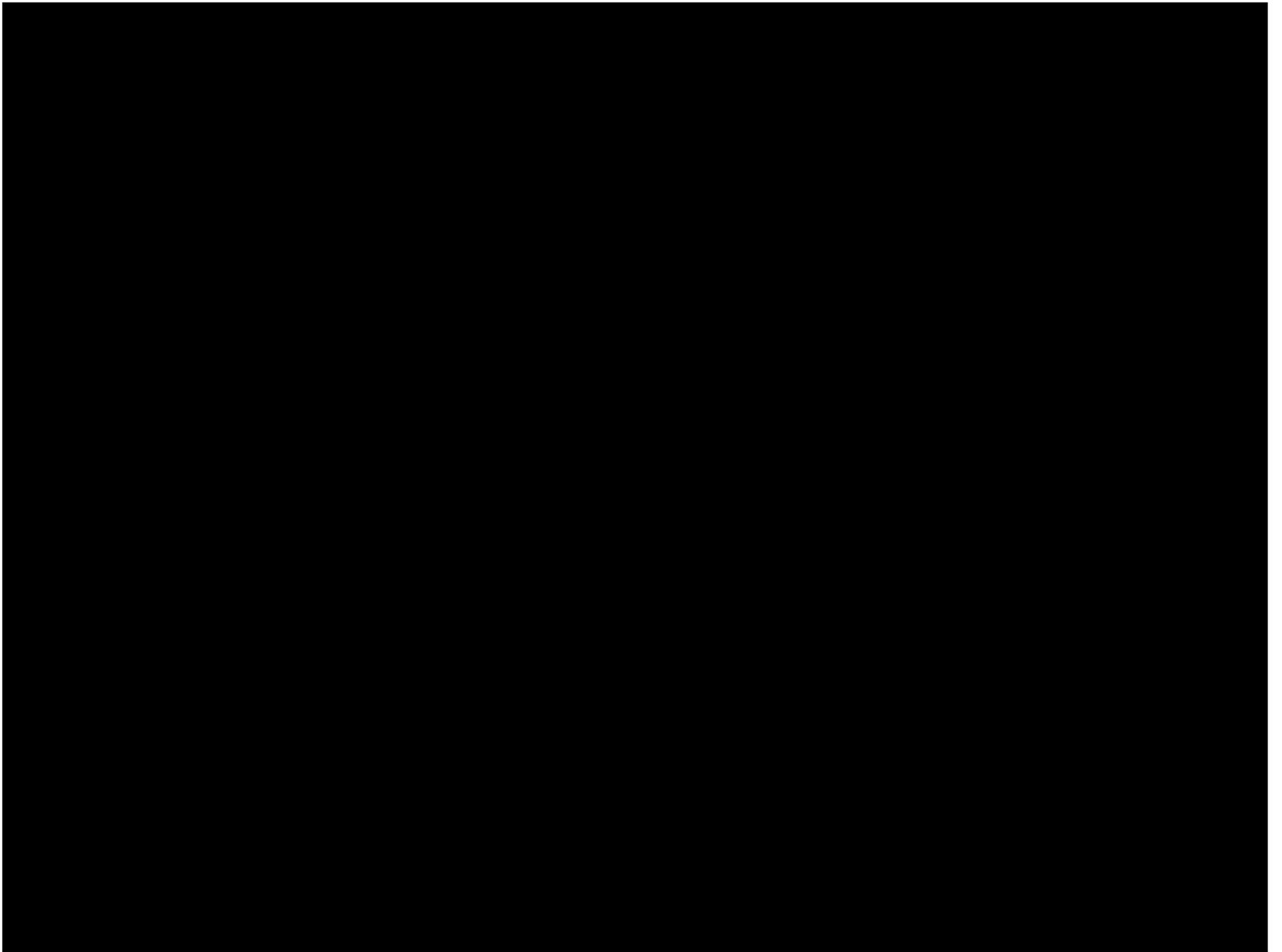
- (1) Correct population-level behavior can result from correct individual-level learning behavior in some cases (small discrepancies compounded over time).
- (2) In the case study examined here, linguistic evolution occurs at the correct rate only when learners employ selective learning biases that cause them to use only a subset of the available data.
- (3) Models of linguistic evolution can be empirically grounded and then more easily manipulated to fit the available data (less parameters of variation).
  - Individual-level:** learning period, data distribution, linguistic representation, probabilistic learning
  - Population-level:** population size, population growth rate, time period of change, rate of change

# Thank You

Amy Weinberg  
Colin Phillips

Norbert Hornstein  
Philip Resnik

the Cognitive Neuroscience of Language Lab  
at the University of Maryland  
Pennsylvania Linguistics Colloquium  
The Northwestern Institute on Complex Systems



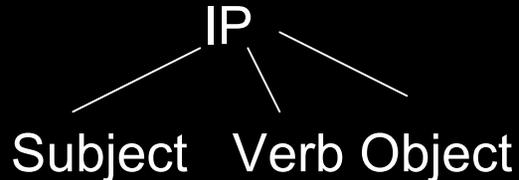
# Individual Framework Applicability

Benefit: Can combine discrete representations, selective learning biases, and probabilistic learning for many types of linguistic knowledge.

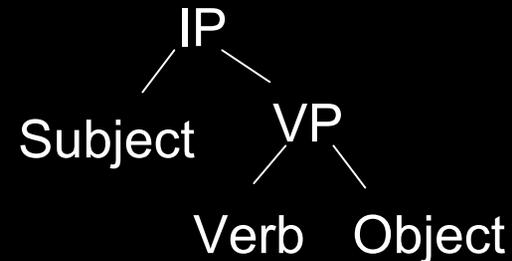


**Discrete Representation:** How much structure is posited for language?

A = linear structure



B = hierarchical structure



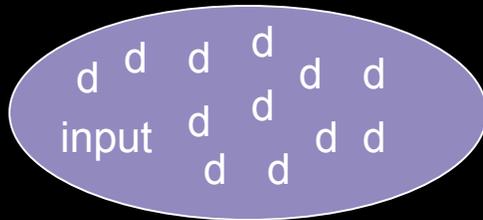
**Discrete Representation :** Is the basic word order Object Verb or Verb Object?

A = Object Verb

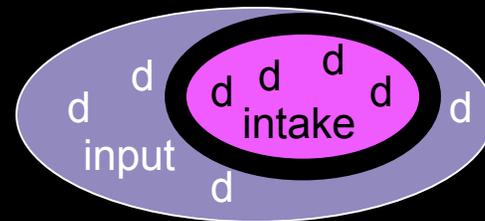
B = Verb Object

# Framework Applicability

Benefit: Can combine discrete representations, selective learning biases, and probabilistic learning for many different problems.



**Learning Bias:** Use all available data. (Good for probabilistic learner - no data sparseness problem.)



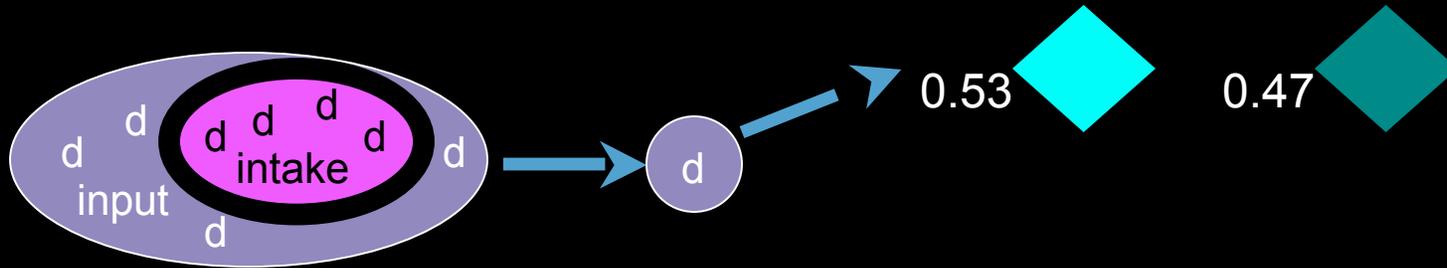
**Selective Learning Bias:** Use only data perceived as most informative (Fodor 1998, Lightfoot 1999, Dresher 1999).

**Selective Learning Bias:** Use only data that is more accessible (perhaps for language processing reasons) (Lightfoot 1991).

**Selective Learning Bias:** Use only data that is perceived as more systematic (Yang 2005).

# Framework Applicability

Benefit: Can combine discrete representations, selective learning biases, and probabilistic learning for many different problems.



This can be instantiated as Bayesian updating, a Linear reward-penalty scheme, or any other probabilistic learning procedure.

$$\text{Max}(\text{Prob}(p_{vo} | u)) = \text{Max}\left(\frac{\text{Prob}(u | p_{vo}) * \text{Prob}(p_{vo})}{\text{Prob}(u)}\right)$$

$$p_{ov} = p_{ov} + \gamma(1 - p_{vo})$$

$$p_{vo} = 1 - p_{ov}$$



# Estimating Historical $p_{VO}$

Known quantities:  
Unambiguous and  
ambiguous data in  
d0 and d1

# Estimating Historical $p_{VO}$

OV Unamb

Amb

VO Unamb

D0

OV Unamb

Amb

VO Unamb

D1

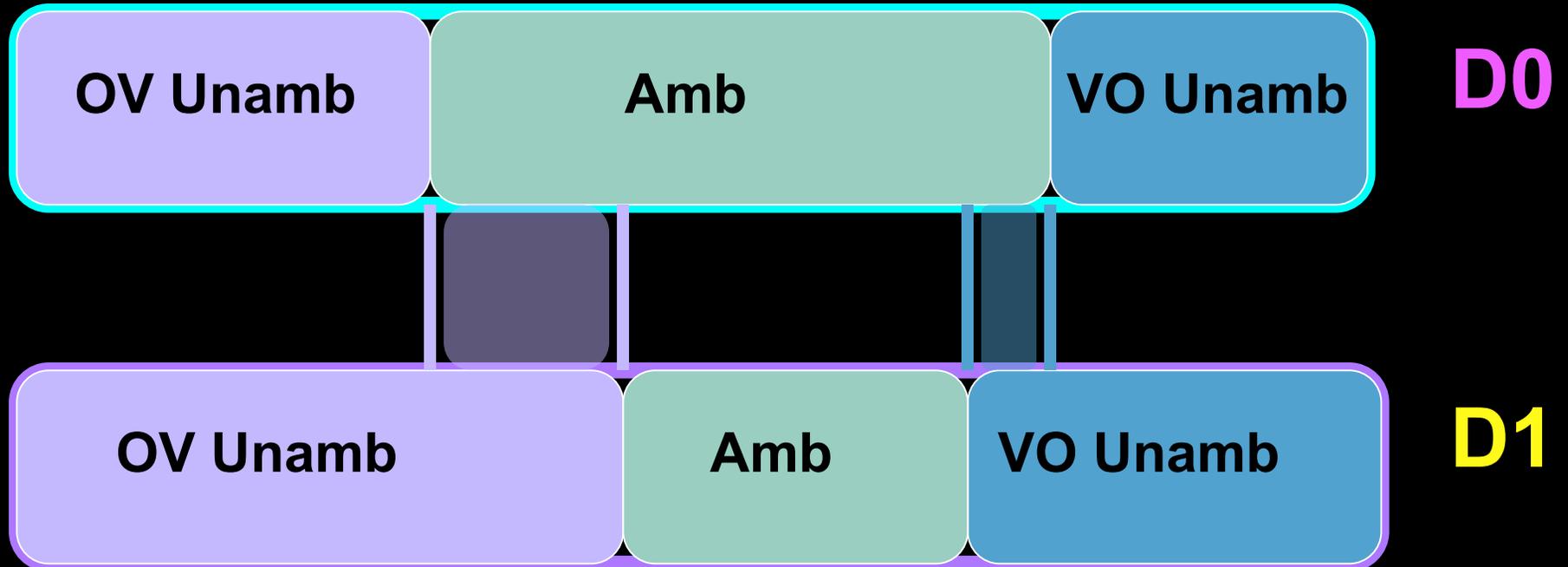
# Estimating Historical $p_{V0}$

Known quantities:  
Unambiguous and  
ambiguous data in  
d0 and d1



Normalize d1 to d0  
distribution: estimate  
how much d1  
unambiguous data was  
“lost” in d0

# Estimating Historical $p_{VO}$



# Estimating Historical $p_{VO}$

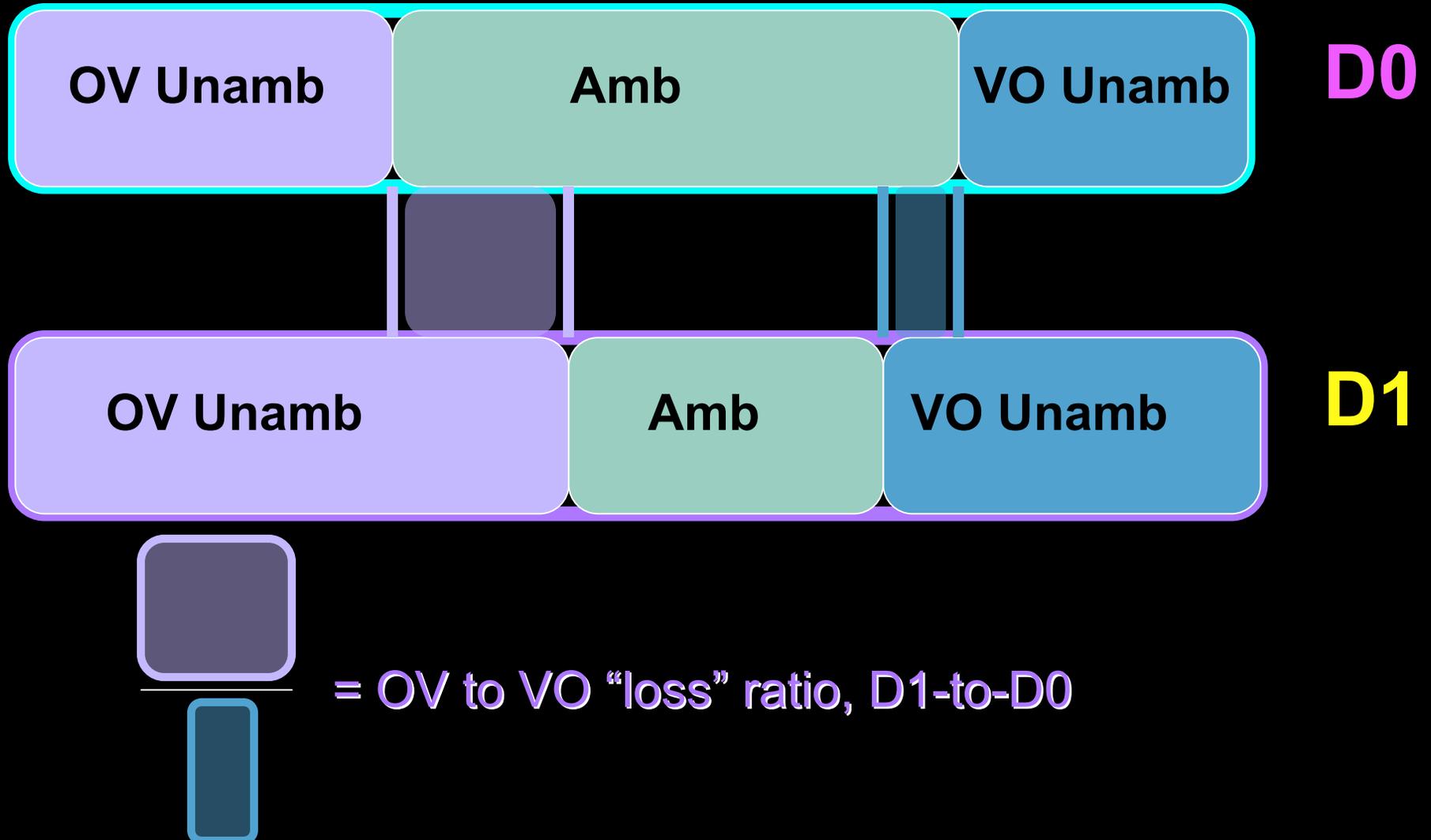
Known quantities:  
Unambiguous and  
ambiguous data in  
d0 and d1

```
graph LR; A[Known quantities:  
Unambiguous and  
ambiguous data in  
d0 and d1] --> B[Normalize d1 to d0  
distribution: estimate  
how much d1  
unambiguous data was  
"lost" in d0]; B --> C[Calculate OV to VO  
"loss ratio"];
```

Normalize d1 to d0  
distribution: estimate  
how much d1  
unambiguous data was  
"lost" in d0

Calculate OV to VO  
"loss ratio"

# Estimating Historical $p_{VO}$



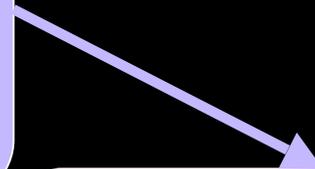
# Estimating Historical $p_{VO}$

Known quantities:  
Unambiguous and  
ambiguous data in  
d0 and d1

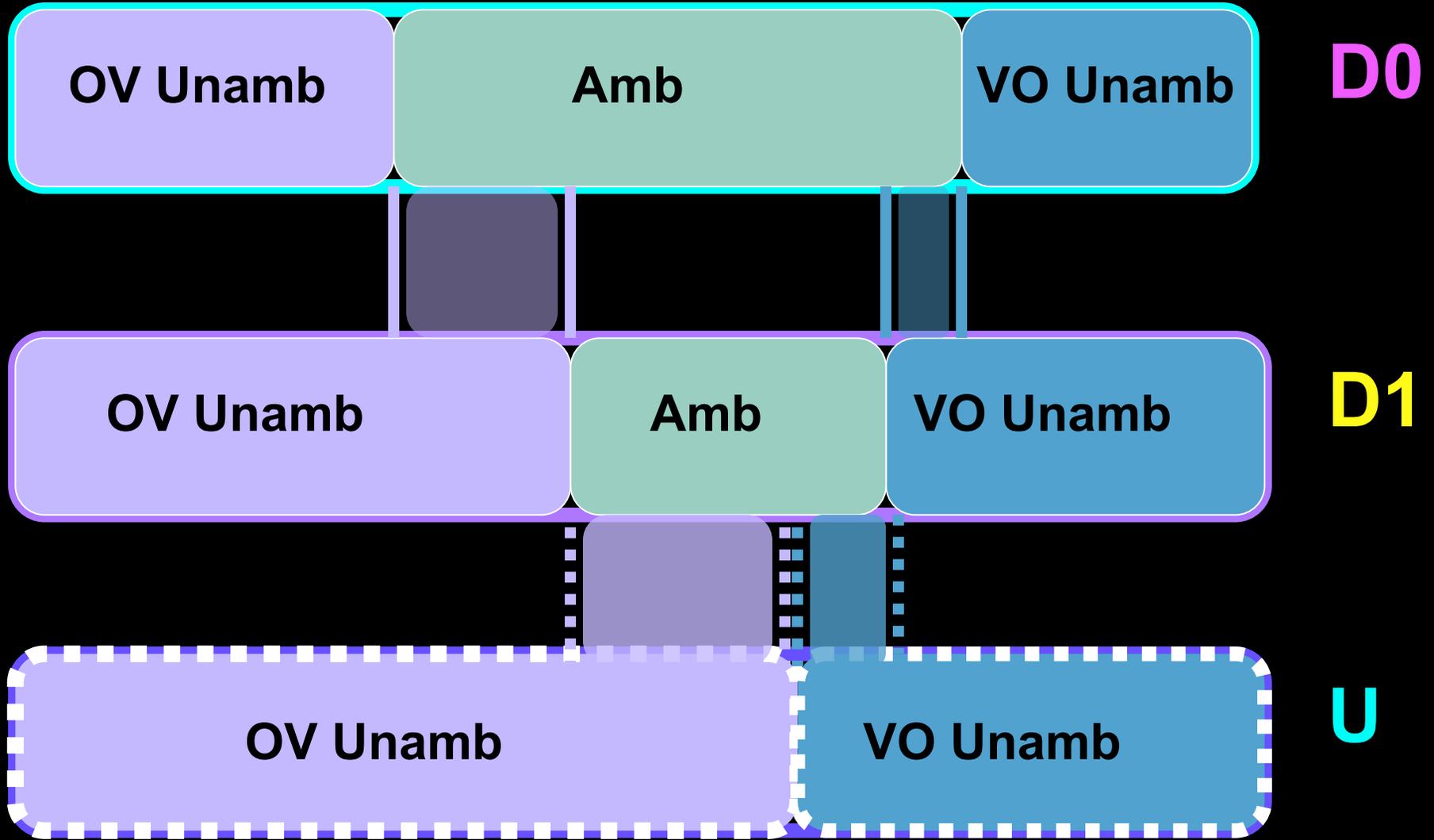
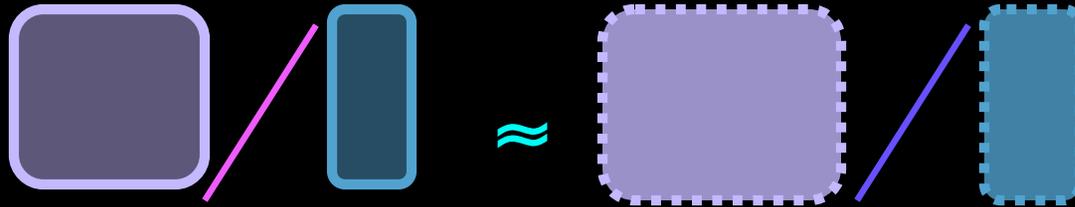
Normalize d1 to d0  
distribution: estimate  
how much d1  
unambiguous data was  
“lost” in d0

Calculate OV to VO  
“loss ratio”

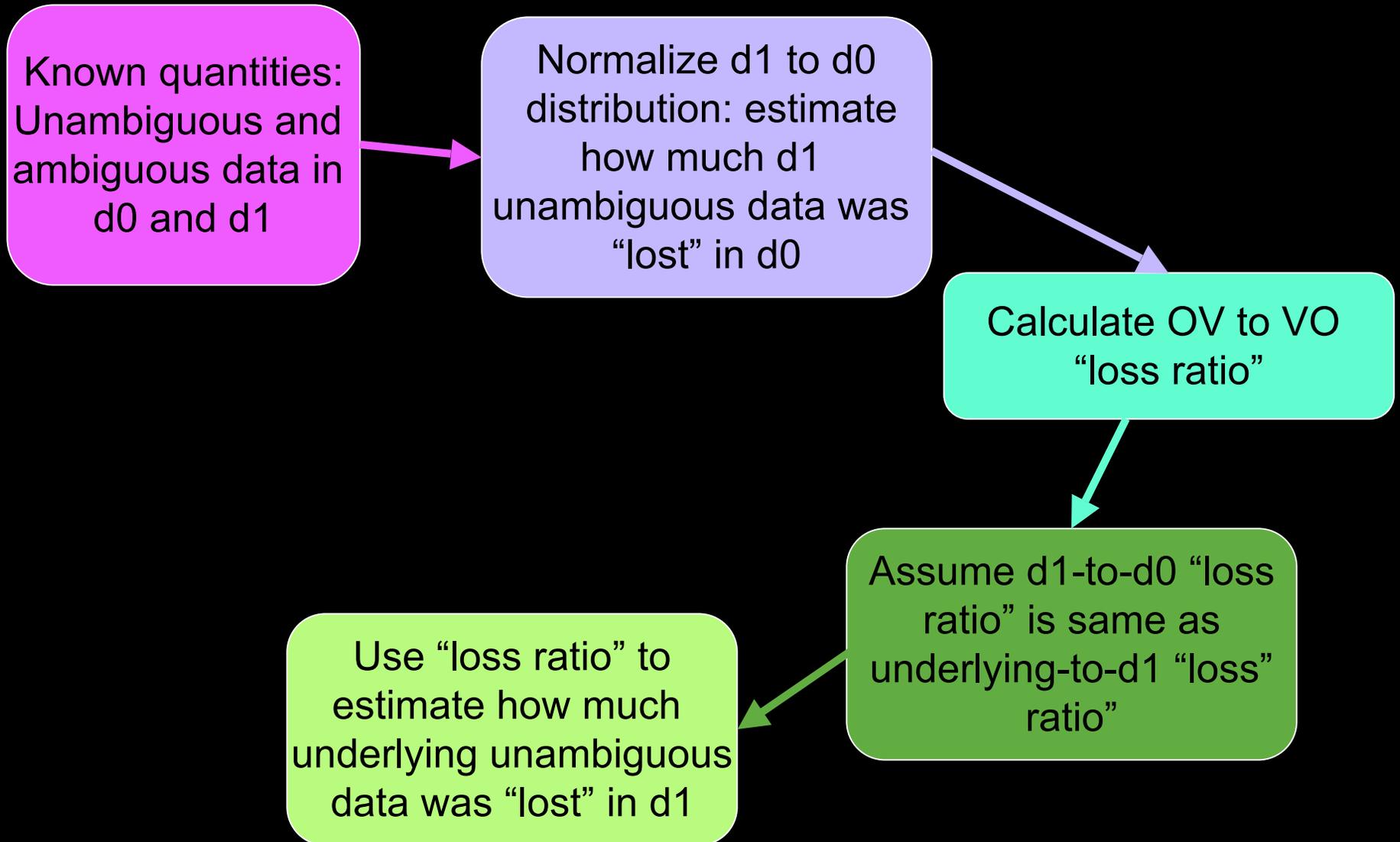
Assume d1-to-d0 “loss  
ratio” is same as  
underlying-to-d1 “loss  
ratio”



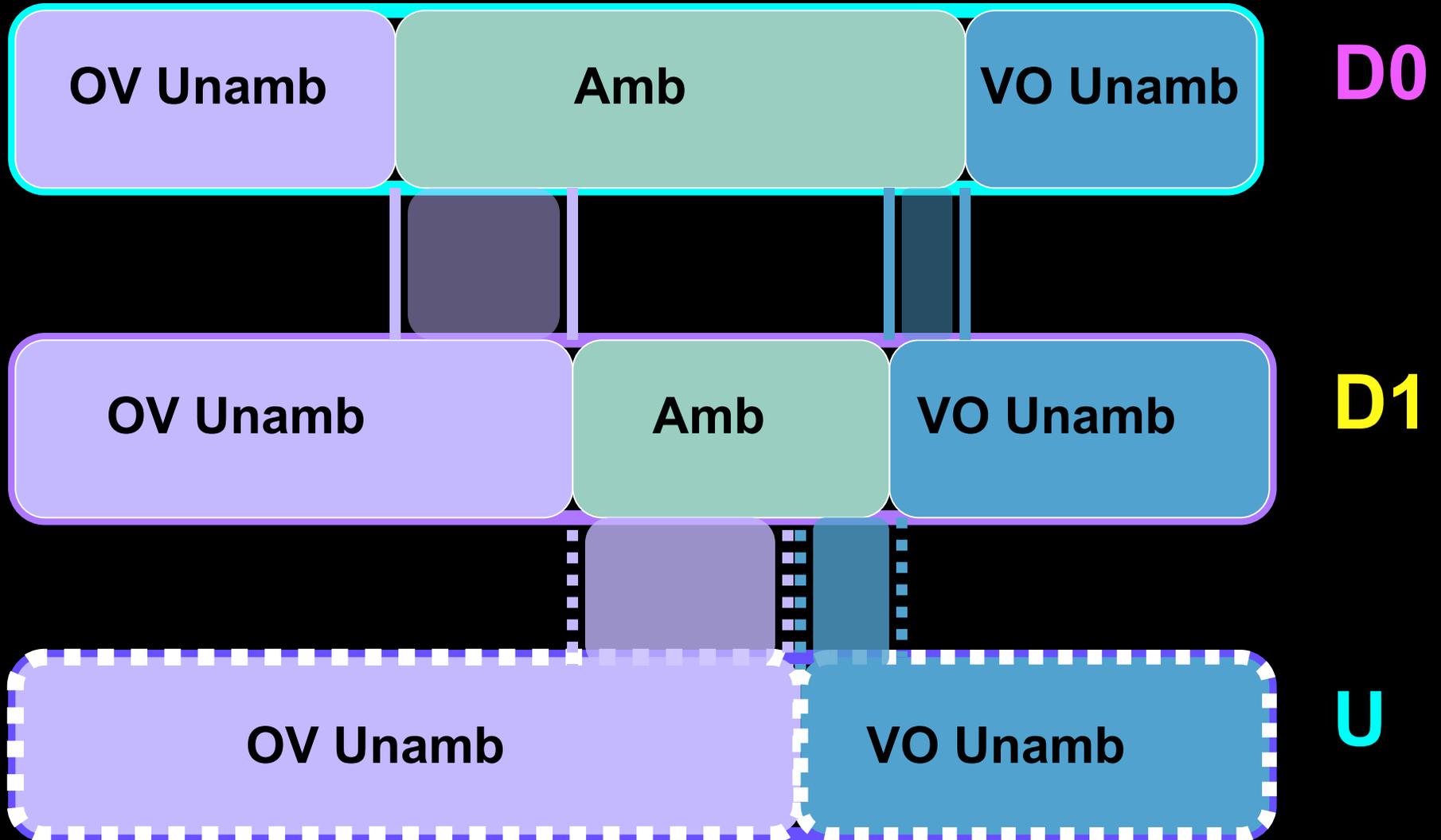
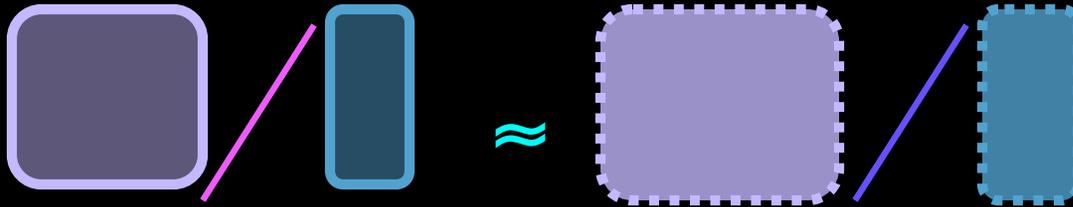
Assumption:



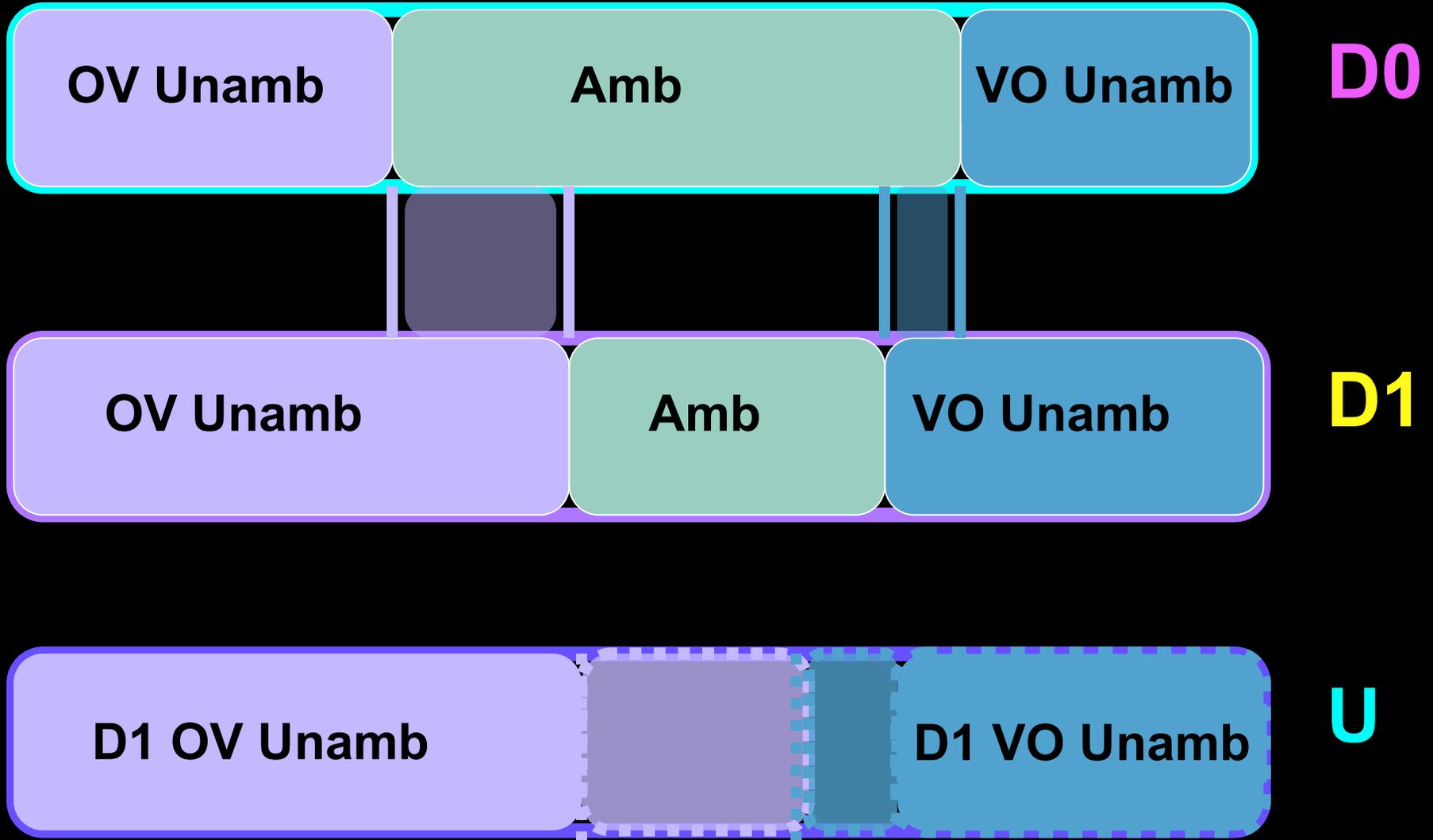
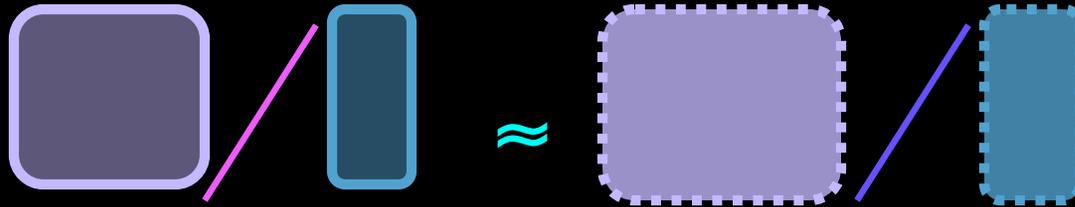
# Estimating Historical $p_{VO}$



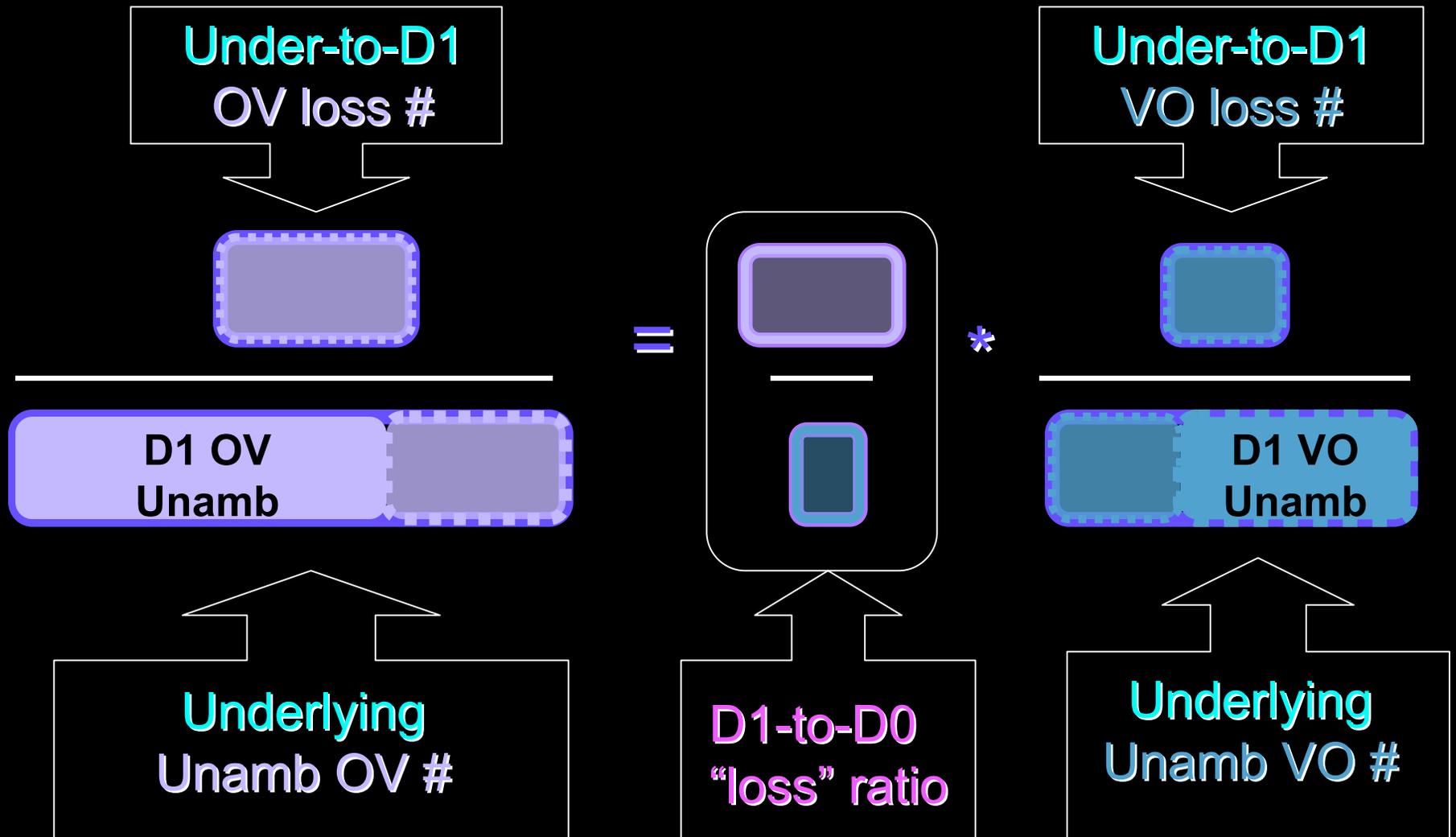
Assumption:



Assumption:



# Estimating Historical $p_{VO}$



# Estimating Historical $p_{VO}$

$$\frac{\gamma * d0 - u1d1'}{\gamma * d0} = Ld1tod0 * \frac{ad1' - (\gamma * d0 - u1d1')}{u2d1' + ad1' - (\gamma * d0 - u1d1')}$$

$\gamma$  = underlying pvo

$d0$  = total degree -0 data,  $d1$  = total degree -1 data

$u1d1'$  = normalized unambiguous OV degree -1 data

$u2d1'$  = normalized unambiguous VO degree -1 data

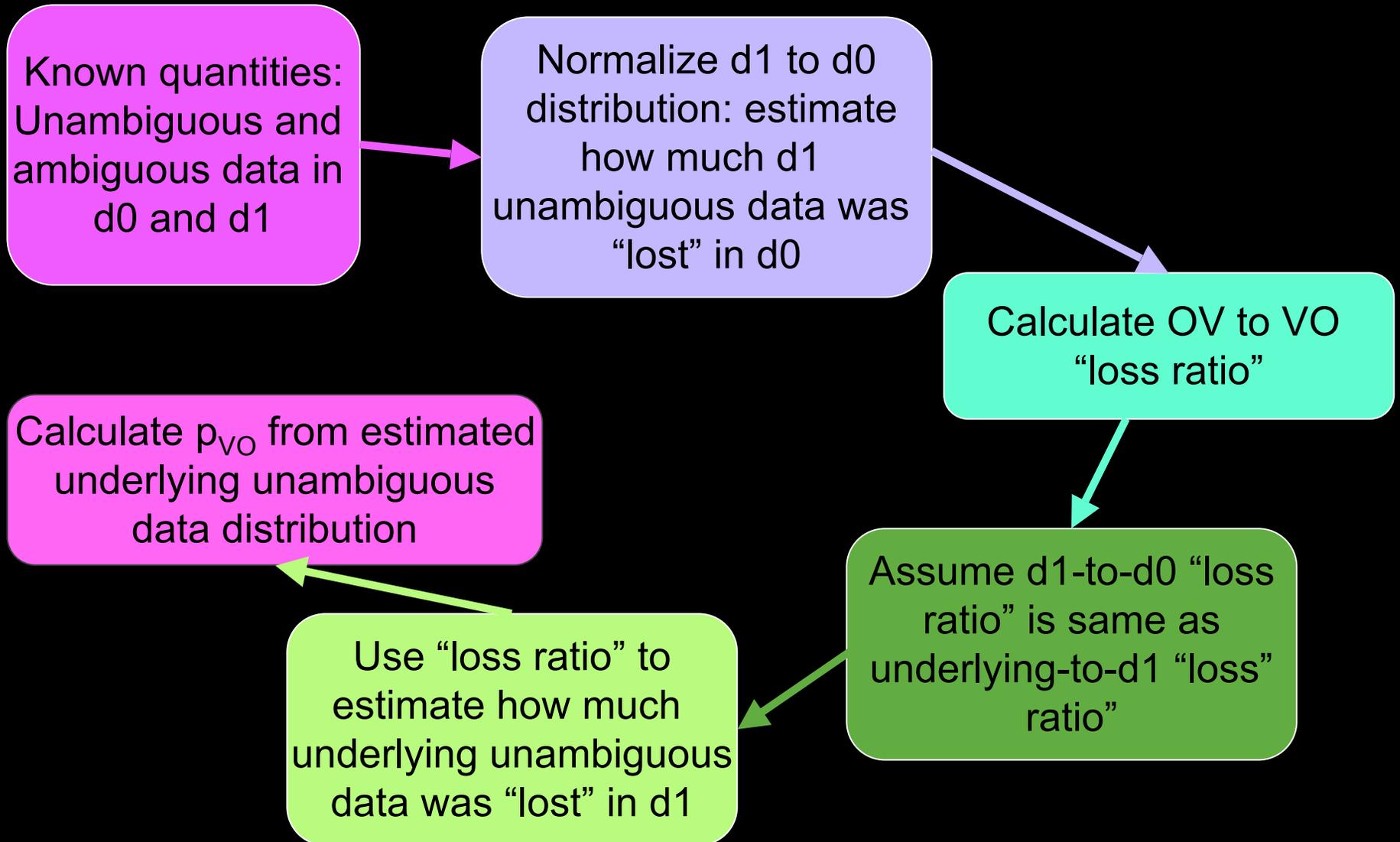
$Ld1tod0$  = loss ratio (OV/VO) from degree -1 to degree -0 distribution

$ad1'$  = normalized ambiguous degree -1 data

$$\gamma = \frac{-(d0)(d0 + u1d1' - Ld1tod0*(ad1' + u1d1'))}{2(Ld1tod0 + 1)(d0^2)}$$

$$+/- \frac{\sqrt{((d0)(d0 + u1d1' - Ld1tod0*(ad1' + u1d1')))^2 - 4(Ld1tod0 + 1)(d0^2)((-1)(d0 * u1d1'))}}{2(Ld1tod0 + 1)(d0^2)}$$

# Estimating Historical $p_{VO}$



# Estimating Historical $p_{VO}$

U OV Unamb

U VO Unamb

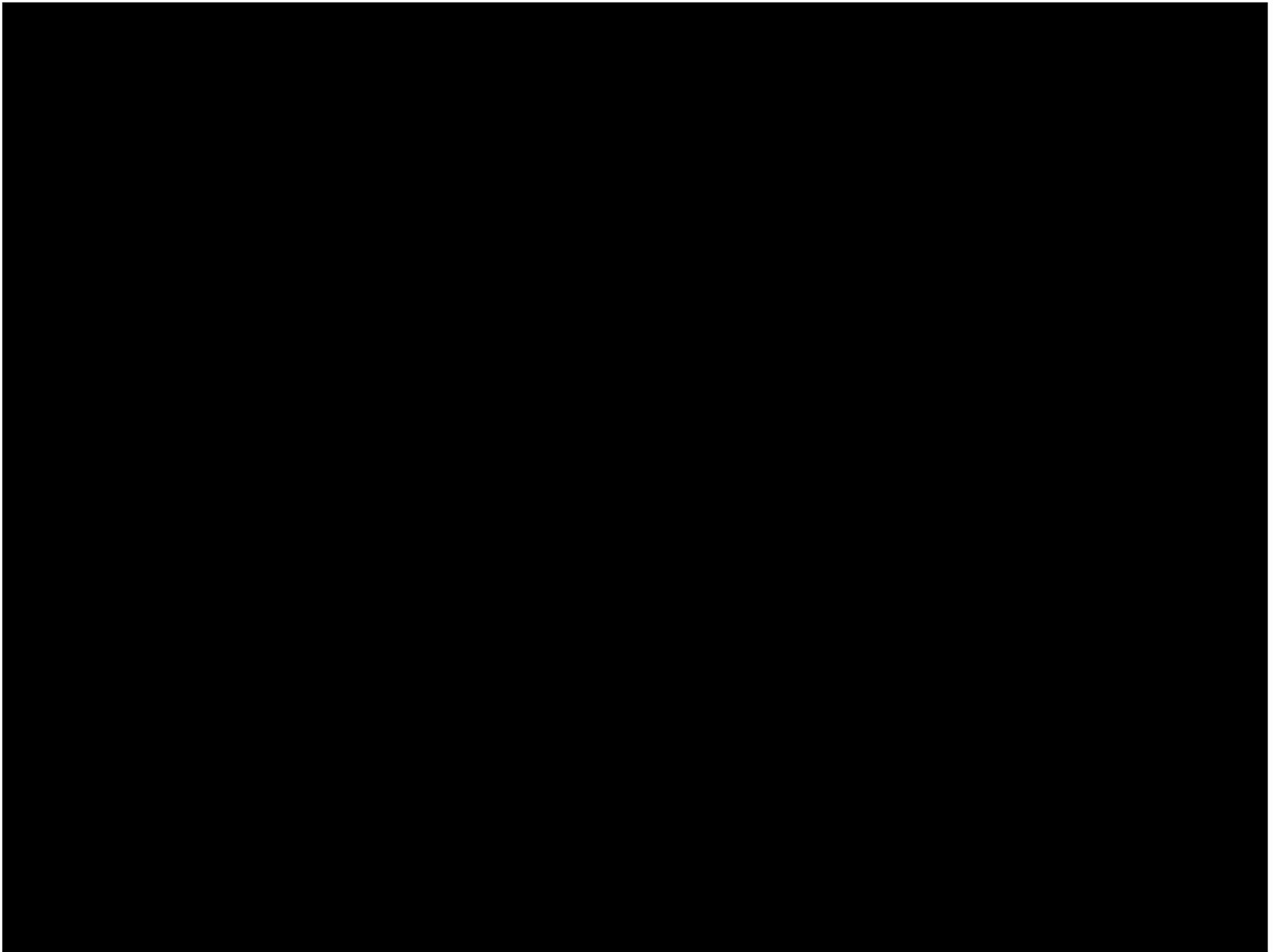
U

U VO Unamb

=  $p_{VO}$

U OV Unamb

U VO Unamb



# Potential Causes of Language Change

Old Norse influence before 1000 A.D.: VO-biased

If sole cause of change, requires exponential influx of Old Norse speakers.

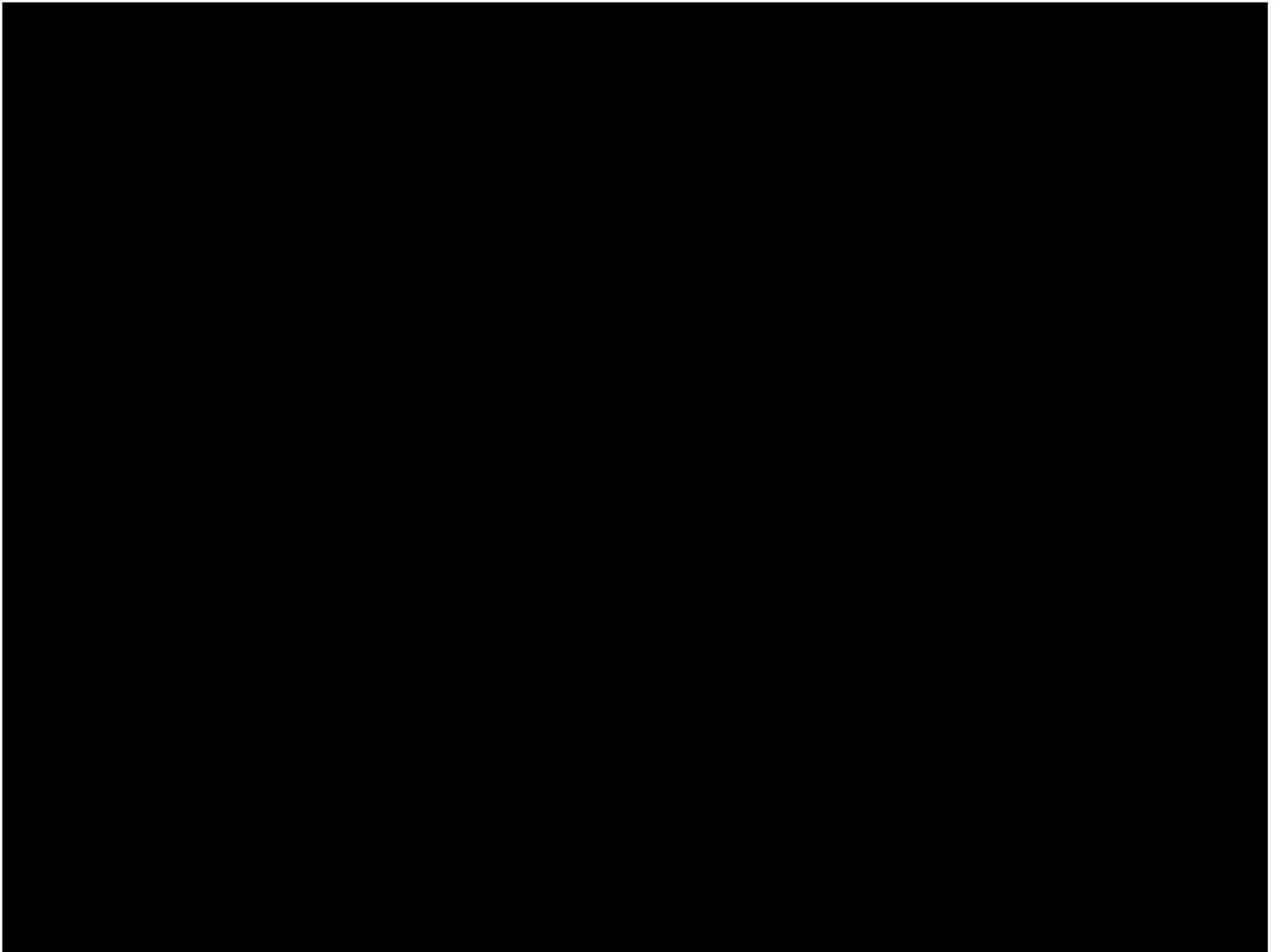
Old French at 1066 A.D.: embedded clauses predominantly OV-biased (Kibler, 1984)

Matrix clauses often SVO (ambiguous)

OV-bias would have hindered Old English change to VO-biased system.

Evidence of individual probabilistic usage in Old English

Historical records likely not the result of subpopulations of speakers who use only one order



# Deriving the Bayesian Update Equations for a Hypothesis Space with 2 Hypotheses

$$\text{Max}(\text{Prob}(p_{vo} | u)) = \text{Max}\left(\frac{\text{Prob}(u | p_{vo}) * \text{Prob}(p_{vo})}{\text{Prob}(u)}\right)$$

Bayes' Rule, find maximum of a posteriori (MAP) probability  
Manning & Schütze (1999)

# Deriving the Bayesian Update Equations for a Hypothesis Space with 2 Hypotheses

$$\text{Max}(\text{Prob}(p_{VO} | u)) = \text{Max}\left(\frac{\text{Prob}(u | p_{VO}) * \text{Prob}(p_{VO})}{\text{Prob}(u)}\right)$$

$\text{Prob}(u | p_{VO})$  = probability of seeing unambiguous data point  $u$ , given  $p_{VO}$   
=  $p_{VO}$

$\text{Prob}(p_{VO})$  = probability of seeing  $r$  out of  $n$  data points that are unambiguous for VO, for  $0 \leq r \leq n$   
=  $\binom{n}{r} * p_{VO}^r * (1 - p_{VO})^{n-r}$

# Deriving the Bayesian Update Equations for a Hypothesis Space with 2 Hypotheses

$$\text{Max}(\text{Prob}(p_{\text{vo}} | u)) = \text{Max}\left(\frac{p_{\text{vo}} * \binom{n}{r} * p_{\text{vo}}^r * (1 - p_{\text{vo}})^{n-r}}{\text{Prob}(u)}\right) \quad (\text{for each point } r, 0 \leq r \leq n)$$

$$\frac{d}{dp_{\text{vo}}} \left( \frac{p_{\text{vo}} * \binom{n}{r} * p_{\text{vo}}^r * (1 - p_{\text{vo}})^{n-r}}{\text{Prob}(u)} \right) = 0$$

$$\frac{d}{dp_{\text{vo}}} \left( \frac{p_{\text{vo}} * \binom{n}{r} * p_{\text{vo}}^r * (1 - p_{\text{vo}})^{n-r}}{\text{Prob}(u)} \right) = 0 \quad (\text{P}(u) \text{ is constant with respect to } p_{\text{vo}})$$

$$p_{\text{vo}} = \frac{r + 1}{n + 1}$$

# Deriving the Bayesian Update Equations for a Hypothesis Space with 2 Hypotheses

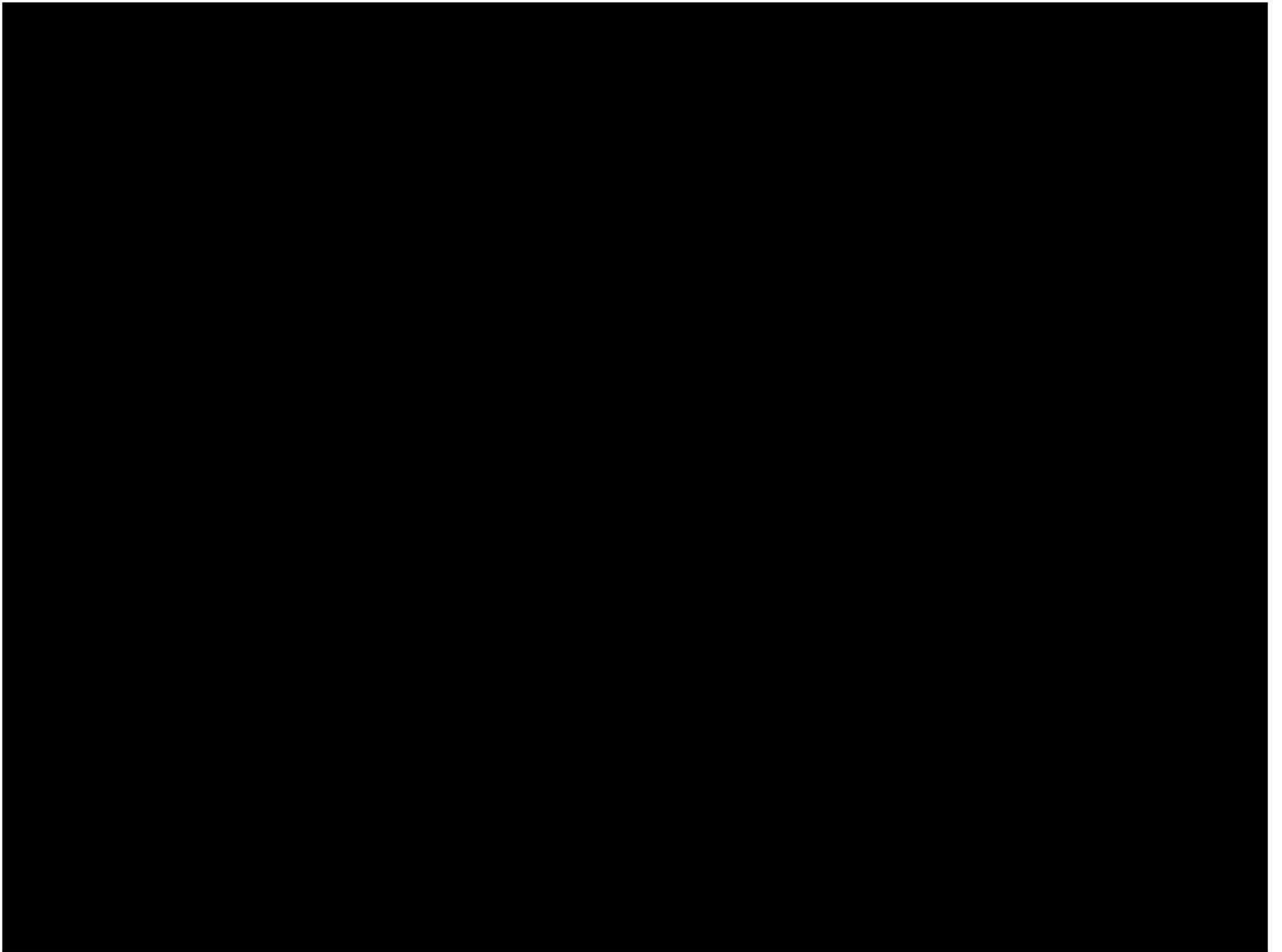
$$p_{VO} = \frac{r + 1}{n + 1}, r = p_{VO_{prev}} * n$$

Replace 1 in numerator and denominator with

$c = p_{VO_{prev}} * m$  if VO,  $c = (1 - p_{VO_{prev}}) * m$  if OV

$$3.0 \leq m \leq 5.0$$

$$p_{VO} = \frac{p_{VO_{prev}} * n + c}{n + c}$$



# Other Ways to Interpret Ambiguous Data

Strategies for assessing ambiguous data

(1) assume base-generation

- attempted and failed
- system-dependent (syntax)

(2) weight based on level of ambiguity (Pearl & Lidz, in submission)

- unambiguous = highest weight
- moderately ambiguous = lower weight
- fully ambiguous = lowest weight (ignore)

(3) randomly assign to one hypothesis (Yang 2002)